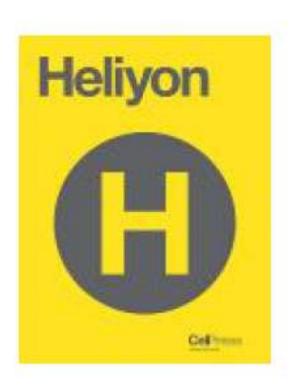
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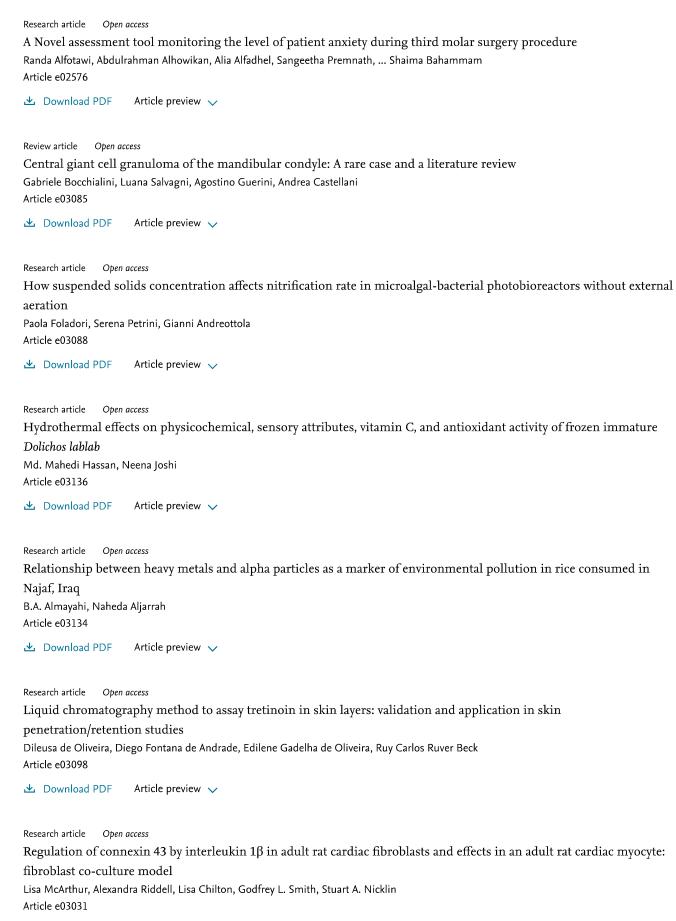
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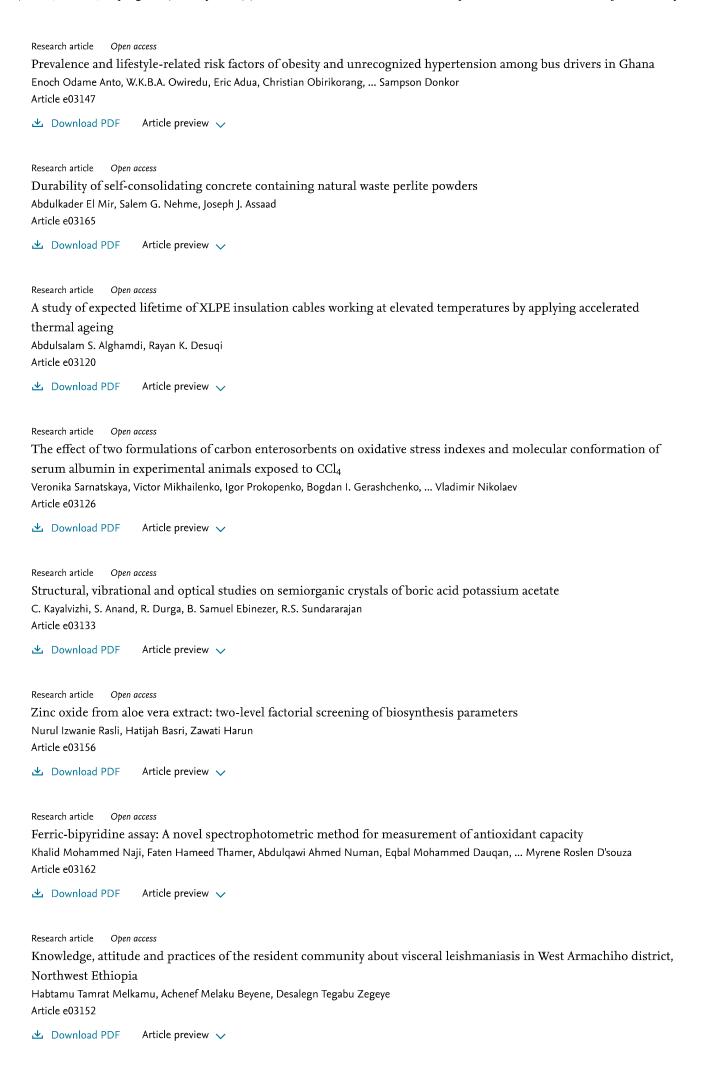
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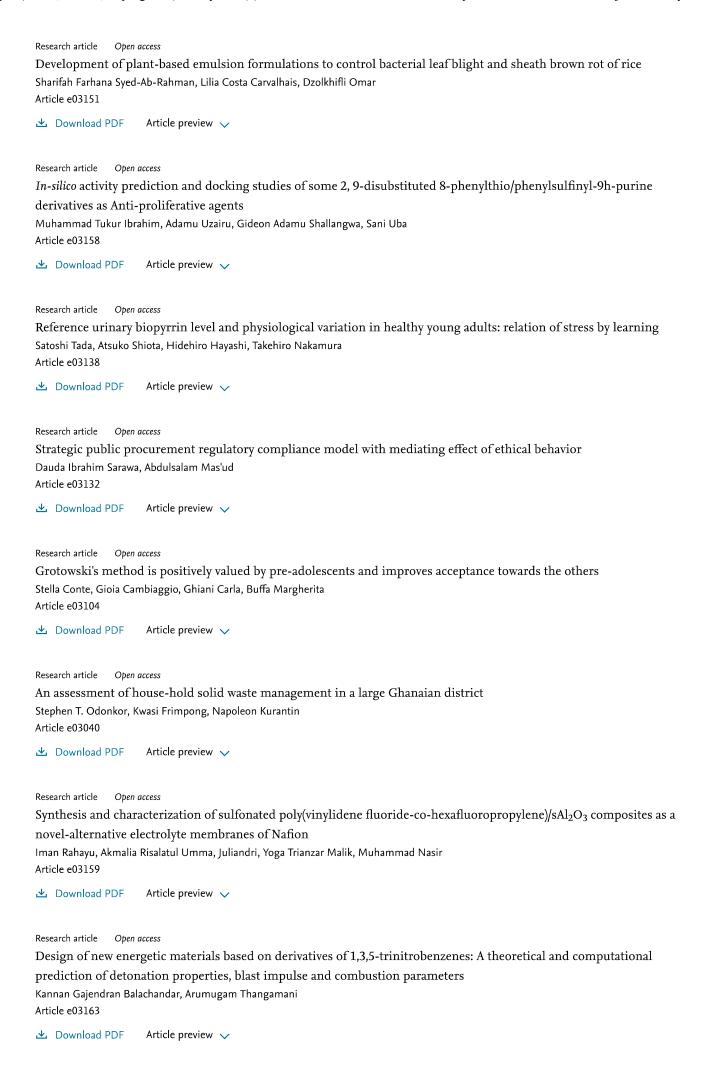
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Research article Optimal control of a discrete age-structured model for tuberculosis transmission

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ABSTRACT

In this present paper, a discrete age-structured model of tuberculosis (TB) transmission is formulated and analyzed. The existence and stability of the model equilibriums are discussed based on the basic reproduction ratio. A sensitivity analysis of the model parameters is determined. We then apply the optimal control strategy for controlling the transmission of TB in child and adult populations. The control variables are TB prevention, chemoprophylaxis of latent TB, and active TB treatment efforts. The optimal controls are then derived analytically using the Pontryagin Maximum Principle. Various intervention strategies are performed numerically to investigate the impact of the interventions. We used the incremental cost-effectiveness ratios (ICER) to assess the benefit of each one the control strategies.

1. Introduction

Tuberculosis (TB) is an airborne infectious disease. It is caused by the bacillus *Mycobacterium tuberculosis*. TB is a major global health problem, and the mortality rate without treatment is high; in fact, TB is one of the top ten diseases causing high mortality. Researchers have found that 70% of people with sputum smear-positive pulmonary TB die within ten years [1]. Based on that prevalence, there were 1.4 million TB deaths and 10.4 million new TB cases, including 5.9 million new cases in men, 3.5 million in women, and 1.0 million in children. The data include 1.2 million HIV-positive patients [1]. About one-third of the world's population has latent TB infections. People with latent TB infections have been infected by the TB bacteria, but they are not infectious [2].

TB attacks both children and adults. Children with latent TB infections are difficult to diagnose. The symptoms of a TB infection in a child only emerge when they have a cough and fever, in some cases it is tied in with influenza. There is little transmission risk, from children with TB. Hence, TB affecting various age groups can indicate a new transmission method [3]. One million children under 14 years have been infected with TB, and 170,000 TB-infected children (excluding children with HIV coinfection) died from the disease in 2015 [2].

Mathematical models have become effective tools with which to understand the dynamics of TB transmission. Some deterministic and stochastic models for TB have been developed to address the spread of the disease, see, for instance, [4, 5]. The model in [4] discussed the dynamics of a TB outbreak by considering the TB treatment effect at home. The stochastic model for a TB outbreak was shown in [5]. Furthermore, mathematical models of a dynamic TB outbreak with optimal control were presented in [6, 7, 8, 9, 10]. The TB model in [6] considered the optimal control for undetected TB cases. The authors in [7] analyzed the optimal strategy to a TB outbreak model by considering the migration of susceptible populations in each area. Silva and Torres discussed an optimal strategy for the TB model with reinfection and post-exposure interventions [8]. The authors in [9] studied optimal control interventions to minimize the number of infectious and latent TB populations using real data from Angola. Rodrigues et al. [10] applied an optimal control problem for TB model with exogenous reinfection. The cost-effectiveness analysis also was done in [10] to in-

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Table 1Parametersmodel (1).	interpretation of the		
Parameter	Interpretation		
Λ	recruitment rate		
θ	immunity loss rate		
β	successful infection rate		
μ	natural death rate		
α	TB progression rate		
γ	recovery rate		
-	1 0		

TB-induced death rate

vestigate the effect of each one of the control strategies, separately or combined.

A number of discrete age-structured mathematical models have been developed for vector-borne diseases such as in [11, 12, 13, 14]. For the epidemic models with direct transmission, most of the age-structured models is formulated in the form of integro-partial differential equations, such as in the TB model [15, 16], HIV model [17], and Buruli ulcer model [18]. Few studies have considered the discrete age-structure of an epidemic model with direct transmission. The authors in [19] investigated an epidemic model as an age-structured TB transmission model in discrete time units and applied it to predict TB infection in China.

In this present paper, we study the dynamics of a TB outbreak within a discrete age-structured population using ordinary differential system. We also explore the impact of the optimal control strategy in reducing latent and active TB populations. The controls are represented by TB prevention, chemoprophylaxis for latent TB, and treatment efforts. The main purpose of optimal control is to reduce latent and active TB populations. The remaining part of the paper is arranged as follows: the formulation of the TB model is addressed in Section 2. The stability analysis and sensitivity analysis of the model parameters are given in Sections 3 and 4. The application of the optimal control problem and the numerical simulation to support the analytic results are shown in Section 5 and 6. The cost-effectiveness discussion is performed in Section 7. The concluding remark is summarized in Section 8.

2. Model formulation

First, we construct a TB spread model by taking into account a single age-structured population. The population is assumed to be closed and is divided into four classes, which are the susceptible class (S), the latent TB class (E), the active TB class (I), and the recovered class (R). The latent TB class consists of hosts infected by TB bacteria, but without an infectious status. The active TB class consists of hosts with infectious status. The single age-structured TB spread model is as follows.

$$\frac{dS}{dt} = \Lambda + \theta R - \beta S I - \mu S,$$

$$\frac{dE}{dt} = \beta S I - (\alpha + \mu) E,$$

$$\frac{dI}{dt} = \alpha E - (\gamma + \mu + d) I,$$

$$\frac{dR}{dt} = \gamma I - (\mu + \theta) R.$$
(1)

We assume that the parameters used in the model equation (1) are constant and non-negative. Moreover, Table 1 consists of the interpretation of the parameters.

Next, we construct a TB spread model by taking into account a discrete age-structured population. This model represents an extension of model (1). We split the population into child (C) and adult (A) populations. Furthermore, each population is partitioned into four classes,

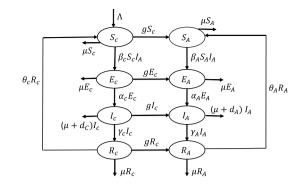


Fig. 1. A discrete age-structured TB transmission diagram.

of model (2)

able 2	
arameters	description

T P

Description	Para	meter
Recruitment rate into the population	1	1
Child survival rate	į	g
Natural death rate	,	и
	Child population	Adult population
Infection rate	β_C	β_A
Progression rate from latent to infectious	α_C	α_A
Natural recovery rate	γ_C	γ_A
Immunity loss rate	θ_{C}	θ_A
TB death rate	d_C	d_A

namely, the susceptible classes (S_C , S_A), the latent TB classes (E_C , E_A), the active TB classes (I_C , I_A), and the recovered classes (R_C , R_A). Therefore, the total size the population is $N = S_C + S_A + E_C + E_A + I_C + I_A + R_C + R_A$. In this second model, we use the average natural death rate of the total population, i.e., the natural death rates of the child and adult populations are assumed to be equal.

Children with TB are less likely to spread the TB bacteria to others [3, 20]. Hence, we assume that the children were infected by TB through contacts with active-TB adults. Hence, only the active TB adults can spread the TB bacteria in the population. The transmission diagram is given in Fig. 1 for deriving a discrete age-structured model. The model is derived as follows.

$$\begin{aligned} \frac{dS_C}{dt} &= \Lambda + \theta_C \ R_C - \beta_C \ S_C \ I_A - (\mu + g) \ S_C, \\ \frac{dS_A}{dt} &= g \ S_C + \theta_A \ R_A - \beta_A \ S_A \ I_A - \mu \ S_A, \\ \frac{dE_C}{dt} &= \beta_C \ S_C \ I_A - (\alpha_C + \mu + g) \ E_C, \\ \frac{dE_A}{dt} &= \beta_A \ S_A \ I_A + g \ E_C - (\alpha_A + \mu) \ E_A, \\ \frac{dI_C}{dt} &= \alpha_C \ E_C - (\gamma_C + \mu + g + d_C) \ I_C, \\ \frac{dI_A}{dt} &= \alpha_A \ E_A + g \ I_C - (\gamma_A + \mu + d_A) \ I_A, \\ \frac{dR_C}{dt} &= \gamma_C \ I_C - (\mu + g + \theta_C) \ R_C, \\ \frac{dR_A}{dt} &= \gamma_A \ I_A + g \ R_C - (\mu + \theta_A) \ R_A. \end{aligned}$$
(2)

All of the parameters used in model (2) are assumed to be constant and non-negative. Their description can be seen in Table 2. Furthermore, model (2) has the region of biological interest as follows.

$$\Omega = \left\{ (S_C, S_A, E_C, E_A, I_C, I_A, R_C, R_A) \in \mathbb{R}^8_+ : 0 \le N \le \frac{\Lambda}{\mu} \right\}$$

Model (2) is well-defined in the region Ω due to the vector field of the model on the boundary of the region Ω does not point to the exterior area. Hence, if we give an initial condition in the region, then the solution of the model is well-defined for all time $t \ge 0$ and remains in the feasible region Ω .

3. Analysis of the model

First, we analyze model (1). Model (1) has two equilibria. Its diseasefree equilibrium is $E_0^s = \left(\frac{\Lambda}{u}, 0, 0, 0\right)$ and its basic reproduction ratio is

$$R_0^s = \frac{\alpha \beta \Lambda}{\mu (\alpha + \mu) (\gamma + \mu + d)}.$$
(3)

The basic reproduction ratio describes the expected number of secondary case from primary case during the infectious period of the primary case [21, 22].

Moreover, model (1) has the endemic equilibrium $E_1^s = \left(\frac{\Lambda}{R_0^s \mu}, E^s, I^s, R^s\right)$, where

$$E^{s} = \frac{(R_{0}^{s} - 1)(\gamma + \mu + d)(\theta + \mu)\Lambda}{R_{0}^{s}[(\theta + \mu)(d(\alpha + \mu) + \mu(\gamma + \mu)) + \alpha\mu(\gamma + \theta + \mu)]},$$

$$I^{s} = \frac{(R_{0}^{s} - 1)(\theta + \mu)\alpha\Lambda}{R_{0}^{s}[(\theta + \mu)(d(\alpha + \mu) + \mu(\gamma + \mu)) + \alpha\mu(\gamma + \theta + \mu)]},$$

$$R^{s} = \frac{(R_{0}^{s} - 1)\alpha\gamma\Lambda}{R_{0}^{s}[(\theta + \mu)(d(\alpha + \mu) + \mu(\gamma + \mu)) + \alpha\mu(\gamma + \theta + \mu)]}.$$

The equilibrium E_0^s is locally asymptotically stable if $R_0^s < 1$, otherwise it is unstable. Furthermore, the equilibrium E_1^s exists and is locally asymptotically stable if $R_0^s > 1$ [23].

0). Furthermore, it has the basic reproduction ratio

$$R_0 = \frac{g \Lambda [\alpha_A \beta_A \eta_2 \eta_4 + \beta_C \mu (\alpha_A \eta_4 + \alpha_C \eta_3)]}{\mu \eta_1 \eta_2 \eta_3 \eta_4 \eta_5},$$
(4)

where $\eta_1 = g + \mu$, $\eta_2 = \alpha_C + \mu + g$, $\eta_3 = \alpha_A + \mu$, $\eta_4 = \gamma_C + \mu + g + d_C$ and $\eta_5 = \gamma_A + \mu + d_A$. The ratio R_0 comes from the 1 × 1 next-generation matrix because only the active TB adult population I_A can spread TB infections. Using Theorem 2 in [23], the equilibrium E_0^t is locally asymptotically stable if $R_0 < 1$, otherwise it is unstable.

In addition to the equilibrium E'_{0} , model (2) also has an endemic equilibrium $E'_{1} = (S'_{C}, S'_{A}, E'_{C}, E'_{A}, I'_{C}, I'_{A}, R'_{C}, R'_{A})$ if $R_{0} > 1$. All of the components of E'_{1} are positive if $R_{0} > 1$. The components depend on the equilibrium state I'_{A} . The equilibrium state I'_{A} is the positive root of the quadratic equation $Ax^{2} + Bx + C = 0$, where

$$\begin{split} A &= \beta_A \,\beta_C \,(\eta_3 \,\eta_5 \,\eta_7 - \alpha_A \,\gamma_A \,\theta_A) \,(\eta_2 \,\eta_4 \,\eta_6 - \alpha_C \,\gamma_C \,\theta_C) > 0, \\ B &= \eta_1 \,\eta_2 \,\eta_4 \eta_6 \,\beta_A \,(\eta_3 \,\eta_5 \,\eta_7 - \alpha_A \,\gamma_A \,\theta_A) \\ &- g \,\beta_A \,\beta_C \,\Lambda (\eta_4 \,\eta_6 \,\eta_7 \,\alpha_A + \eta_3 \,\eta_6 \,\eta_7 \,\alpha_C + \alpha_A \,\alpha_C \,\gamma_C \,\theta_A) \\ &+ \eta_3 \,\eta_5 \,\eta_7 \,\beta_C \,\mu \,(\eta_2 \,\eta_4 \,\eta_6 - \alpha_C \,\gamma_C \,\theta_C), \end{split}$$

$$C = -(R_0 - 1) \,\mu \,\eta_1 \,\eta_2 \,\eta_3 \,\eta_4 \,\eta_5 \,\eta_6 \,\eta_7,$$

where $\eta_6 = \mu + g + \theta_C$ and $\eta_7 = \mu + \theta_A$. The coefficient *C* has negative value if $R_0 > 1$. Hence, $I_A^t > 0$ if $R_0 > 1$.

The equilibrium E_1^t is locally asymptotically stable if $R_0 > 1$. The bifurcation diagram of model (2) with respect the ratio R_0 can be seen in Fig. 2.

4. Sensitivity analysis of parameters

In the present section, we implement a sensitivity analysis of the parameters from models (1) and (2). This allows us to determine the

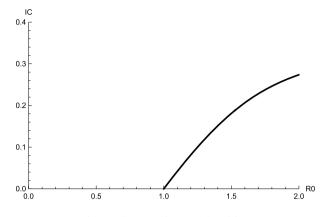


Fig. 2. Bifurcation diagram of model (2).

Table 3	
Parameter values for simulations.	

Parameter	Value	Ref.	Parameter	Value	Ref.
Λ	1000	Assumed	γ_A	0.21	[34]
g	$\frac{1}{14}$	[2]	γ_C	0.2	[34]
β	0.02	[33]	θ_A	0.873	Assumed
β_A	0.02	[33]	θ_{C}	0.83	Assumed
β_C	0.01	[33]	μ	0.0143	[35]
α	0.005	[35]	d	0.05751	[36]
α_A	0.005	[35]	d_A	0.05751	[36]
α_{C}	0.005	[35]	d _C	0.0575	[36]
γ	0.21	[34]	-		

Table 4	
Sensitivity index of the parameters in models (1) and (2).	

Parameter (p)	Sensitivity index $\Upsilon_p^{R_0^s}$	Parameter (p)	Sensitivity index $\Upsilon_p^{R_0}$
Λ	1	Λ	1
β	1	g	0.000105
α	0.7409	β_A	0.923
γ	-0.7452	β_C	0.0768
μ	-1.7917	α_A	0.7379
d	-0.2041	α_C	-0.000143
		γ_A	-0.745
		γ_C	-0.00238
		μ	-1.89
		d_A	-0.204
		d _C	-0.000685

parameters that have a great influence on the basic reproduction ratios (R_0^s and R_0). We adopt the same approach in [24] to derive the analytic formulation for the sensitivity index of R_0^s and R_0 to each parameter. The sensitivity index of Q related to parameter k, is defined as

$$\Upsilon_{k}^{Q} := \frac{\partial Q}{\partial k} \times \frac{k}{Q}.$$
(5)

The sensitivity indices $\Upsilon_{\Lambda}^{R_0^s}$, $\Upsilon_{\beta}^{R_0^s}$, $\Upsilon_{\Lambda}^{R_0}$ are equal to one and do not depend on the values of the other parameters. The sensitivity indices of R_0^s and R_0 related to the remaining parameters can be calculated in the same way as in (5). Using the parameter values in Table 3, their sensitivity indices are given in Table 4.

A positive index indicates that the value of R_0^s or R_0 increases as a parameter is increased. To the contrary, a negative index means that the value of R_0^s or R_0 decreases as a parameter is increased. The sensitivity index of $\Upsilon_{\beta_A}^{R_0} = 0.923$ means that an increase of 10% in the value β_A will increase R_0 by 9.23%. Likewise, a sensitivity index of $\Upsilon_{\gamma_A}^{R_0} = -0.745$ indicates that an increase of 10% in the value γ_A will decrease R_0 by 7.45%.

Next, we compare the sensitivity indices of basic reproduction ratios of models (1) and (2) with respect to some parameters. From Table 4, it can be seen that, when using model (1), the sensitivity indices of the basic reproduction ratio R_0^s with respect to the TB infection rate (β) and the TB progression rate (α) are 1 and 0.7409, respectively. While, for model (2), the sensitivity indices of the basic reproduction ratio R_0 with respect to the TB infection rates for adults (β_A) and children (β_C) are significantly different, i.e., 0.923 and 0.0768, respectively. Similarly, the sensitivity indices of the basic reproduction ratio R_0 with respect to TB progression for adults (α_A) and children (α_C) are 0.7379 and -0.000143, respectively. The significant difference in sensitivity indice values is due to the fact that only active TB adults can spread TB in the population. Hence, the discrete age-structured model provides a more realistic description of TB transmission in the population.

5. Formulation of the optimal control

In the present section, we propose the optimal control problem of the spread of TB within the discrete age-structured model. The control aspect to be optimized in this work is the prevention efforts (u_1) for the susceptible population, chemoprophylaxis (u_2) for the latent TB population, and treatment (u_3) for the active TB population. All of the controls are incorporated into the child and adult populations. The TB spread model involving the discrete age-structured population with three controls is as follows.

$$\frac{dS_C}{dt} = \Lambda + \theta_C R_C - (1 - u_1) \beta_C S_C I_A - (\mu + g) S_C,$$

$$\frac{dS_A}{dt} = g S_C + \theta_A R_A - (1 - u_1) \beta_A S_A I_A - \mu S_A,$$

$$\frac{dE_C}{dt} = (1 - u_1) \beta_C S_C I_A - (\alpha_c + \mu + g) E_C - \delta_C u_2 E_C,$$

$$\frac{E_A}{dt} = (1 - u_1) \beta_A S_A I_A + g E_C - (\alpha_A + \mu) E_A - \delta_A u_2 E_A,$$

$$\frac{dI_C}{dt} = \alpha_C E_C - (\gamma_c + \mu + g + d_C) I_C - b_C u_3 I_C,$$

$$\frac{dI_A}{dt} = \alpha_A E_A + g I_C - (\gamma_A + \mu + d_A) I_A - b_A u_3 I_A,$$

$$\frac{dR_C}{dt} = \gamma_C I_C - (\mu + g + \theta_C) R_C + \delta_C u_2 E_C + b_C u_3 I_C,$$
(6)

The parameters δ_C and δ_A represent the recovery rate from chemoprophylaxis for the child and adult populations, respectively. Moreover, the parameters b_C and b_A denote the recovery rate from treatment for the child and adult populations, respectively. We could obtain the optimal control strategies by minimizing following cost function.

$$J(u_1, u_2, u_3) = \int_{0}^{I_f} E_c + E_A + I_c + I_A + \frac{c_1}{2}u_1^2 + \frac{c_2}{2}u_2^2 + \frac{c_3}{2}u_3^2 dt,$$
(7)

where c_1 , c_2 , and c_3 are weighting constants for the TB prevention efforts, chemoprophylaxis of latent TB, and treatment for active TB, respectively.

We use a quadratic form to measure the control costs [25, 26, 27, 28]. The terms $c_1 u_1^2, c_2 u_2^2$ and $c_3 u_3^2$ depict the costs correlated with the TB prevention, chemoprophylaxis, and TB treatment controls, respectively. Thus, greater values of c_1 , c_2 , and c_3 will indicate higher implementation costs for the prevention of TB, chemoprophylaxis, and treatment, respectively.

We seek the optimal controls u_1^* , u_2^* , and u_3^* such that

$$J(u_1^*, u_2^*, u_3^*) = \underbrace{min}_{\Gamma} J(u_1, u_2, u_3),$$
(8)

where $\Gamma = \{(u_1, u_2, u_3) | 0 \le u_i \le 1, i = 1, 2, 3\}$. In this region, when the value of a control is zero, then no investment in control have been made. Moreover, when the value of a control is one, then a control effort has been carried out maximally.

The conditions necessary for determining the optimal controls u_1^* , u_2^* , and u_3^* that satisfy condition (8) with constraint model (6) will be found via Pontryagin's Maximum Principle [29]. This principle converts equations (6), (7), and (8) into a problem of minimizing the Hamiltonian function *H*, pointwise with respect to (u_1, u_2, u_3) , i.e.,

$$H = E_c + E_A + I_c + I_A + \frac{c_1}{2}u_1^2 + \frac{c_2}{2}u_2^2 + \frac{c_3}{2}u_3^2 + \sum_{i=1}^8 \lambda_i f_i,$$

where f_i denotes the right-hand side of model (6). The adjoint variables λ_i for i = 1, 2, ..., 8 satisfy the following co-state system.

$$\begin{split} \dot{\lambda_{1}} &= -\frac{\partial H}{\partial S_{C}} = \lambda_{1} \left[(1-u_{1}) \beta_{C} I_{A} + \mu + g \right] - \lambda_{2} g - \lambda_{3} (1-u_{1}) \beta_{C} I_{A}, \\ \dot{\lambda_{2}} &= -\frac{\partial H}{\partial S_{A}} = \lambda_{2} \left[(1-u_{1}) \beta_{A} I_{A} + \mu \right] - \lambda_{4} (1-u_{1}) \beta_{A} I_{A}, \\ \dot{\lambda_{3}} &= -\frac{\partial H}{\partial E_{C}} = -1 + \lambda_{3} (\delta_{C} u_{2} + g + \mu + \alpha_{C}) - \lambda_{4} g - \lambda_{5} \alpha_{C} - \lambda_{7} \delta_{C} u_{2}, \\ \dot{\lambda_{4}} &= -\frac{\partial H}{\partial E_{A}} = -1 + \lambda_{4} (\delta_{A} u_{2} + \mu + \alpha_{A}) - \lambda_{6} \alpha_{A} - \lambda_{8} \delta_{A} u_{2}, \\ \dot{\lambda_{5}} &= -\frac{\partial H}{\partial I_{C}} = -1 + \lambda_{5} (b_{C} u_{3} + g + \mu + \gamma_{C} + d_{C}) - \lambda_{6} g - \lambda_{7} (b_{C} u_{3} + \gamma_{C}), \quad (9) \\ \dot{\lambda_{6}} &= -\frac{\partial H}{\partial I_{A}} = -1 + (\lambda_{1} - \lambda_{3})(1 - u_{1}) \beta_{C} S_{C} + (\lambda_{2} - \lambda_{4})(1 - u_{1}) \beta_{A} S_{A} \\ &\quad + (\lambda_{6} - \lambda_{8})(\gamma_{A} + b_{A} u_{3}) + \lambda_{6}(\mu + d_{A}), \\ \dot{\lambda_{7}} &= -\frac{\partial H}{\partial R_{C}} = -\lambda_{1} \theta_{C} + \lambda_{7} (\mu + g + \theta_{C}) - \lambda_{8} g, \\ \dot{\lambda_{8}} &= -\frac{\partial H}{\partial R_{A}} = -\lambda_{2} \theta_{A} + \lambda_{8} (\mu + \theta_{A}), \end{split}$$

where the transversality conditions $\lambda_i(t_f) = 0, i = 1, 2, ..., 8$.

The steps needed to obtain the optimal controls $u = (u_1^*, u_2^*, u_3^*)$ are as follows [30, 31].

1. Minimize the Hamiltonian function H with respect to u. We obtain

$$u_{1}^{*} = \begin{cases} 0, & \text{for } u_{1} \leq 0 \\ \frac{I_{A}[(\lambda_{3} - \lambda_{1})\beta_{C}S_{C} + (\lambda_{4} - \lambda_{2})\beta_{A}S_{A}]}{c_{1}}, & \text{for } 0 < u_{1} < 1 \\ 1, & \text{for } u_{1} \geq 1 \end{cases}$$

$$u_{2}^{*} = \begin{cases} 0, & \text{for } u_{2} \leq 0\\ \frac{E_{A}\delta_{A}\lambda_{4} - E_{A}\delta_{A}\lambda_{8} + E_{C}\delta_{C}\lambda_{3} - E_{C}\delta_{C}\lambda_{7}}{c_{2}}, & \text{for } 0 < u_{2} < 1\\ 1, & \text{for } u_{2} \geq 1 \end{cases}$$

$$u_{3}^{*} = \begin{cases} 0, & \text{for } u_{3} \leq 0\\ \frac{I_{A} b_{A} \lambda_{6} - I_{A} b_{A} \lambda_{8} + I_{C} b_{C} \lambda_{5} - I_{C} b_{C} \lambda_{7}}{c_{3}}, & \text{for } 0 < u_{3} < 1\\ 1, & \text{for } u_{3} \geq 1 \end{cases}$$

2. Solve the state system $\dot{x}(t) = \frac{\partial H}{\partial \lambda}$, where $x = (S_c, S_A, E_c, E_A, I_c, I_A, R_c, R_A)$, $\lambda = (\lambda_1, \lambda_2, \dots, \lambda_8)$, using the initial condition x_0 .

3. Solve the co-state system $\dot{\lambda}(t) = -\frac{\partial H}{\partial x}$ with transversality conditions $\lambda_i(t_f) = 0$, for i = 1, 2, 3, ..., 8.

Based on the above steps, the optimum control (u_1^*, u_2^*, u_3^*) is given in the following theorem.

Theorem 1. The optimal control (u_1^*, u_2^*, u_3^*) minimizing the cost function $J(u_1, u_2, u_3)$ on Γ is

$$\begin{split} u_{1}^{*} &= \max\left\{0, \min\left\{1, \frac{I_{A}[(\lambda_{3} - \lambda_{1})\beta_{C}S_{C} + (\lambda_{4} - \lambda_{2})\beta_{A}S_{A}]}{c_{1}}\right\}\right\}\\ u_{2}^{*} &= \max\left\{0, \min\left\{1, \frac{E_{A}\delta_{A}\lambda_{4} - E_{A}\delta_{A}\lambda_{8} + E_{C}\delta_{C}\lambda_{3} - E_{C}\delta_{C}\lambda_{7}}{c_{2}}\right\}\right\}\\ u_{3}^{*} &= \max\left\{0, \min\left\{1, \frac{I_{A}b_{A}\lambda_{6} - I_{A}b_{A}\lambda_{8} + I_{C}b_{C}\lambda_{5} - I_{C}b_{C}\lambda_{7}}{c_{3}}\right\}\right\}\end{split}$$

where λ_i , i = 1, 2, 3, ..., 8, are the solutions of co-state system (9).

Next, the solutions of the optimal system will be solved numerically for various strategies.

6. Numerical results

In the present section, we demonstrate the comparison of the numerical results of the model with control (6) and the model without control (2). We use the fourth order Runge-Kutta (RK4) scheme to solve the optimal control strategy. First, we implement the forward RK4 scheme to solve the state systems. After that, we utilize the backward RK4 scheme to solve the co-state system. We update the controls until the current state, the adjoint, and the control values converge sufficiently [32].

Parameters used for the simulations could be seen in Table 3, for which the basic reproduction ratio $R_0 = 104.51$. We also employed parameters values $\delta_A = 0.7$, $\delta_C = 0.7$, $b_A = 0.55$ and $b_C = 0.55$ [34]. Moreover, the initial condition is $S_C(0) = 3000$, $S_A(0) = 5000$, $E_C(0) = 100$, $E_A(0) = 150$, $I_C(0) = 100$, $I_A(0) = 160$, $R_C(0) = 50$, $R_A(0) = 55$. We assume that $c_3 > c_2 > c_1$. This assumption is based on the facts that the cost associated with treatment for active TB is more expensive than treatment for latent TB, while the cost associated with prevention is cheaper than the treatment for latent TB. Hence, the weighting constants in the objective function are $c_1 = 50$, $c_2 = 70$ and $c_3 = 90$. We investigate four control strategies which are given as follows.

- 1. Combination of TB prevention (u_1) and chemoprophylaxis for latent TB (u_2) .
- 2. Combination of TB prevention (u_1) and active TB treatment (u_3) .
- 3. Combination of chemoprophylaxis for latent TB (u_2) and active TB treatment (u_3) .
- 4. Combination of TB prevention (u_1) , chemoprophylaxis for latent TB (u_2) , and active TB treatment (u_3) .

6.1. First strategy

In the first strategy, combination of TB prevention (u_1) and chemoprophylaxis for latent TB (u_2) is used. Meanwhile, the TB treatment control is not used $(u_3 = 0)$. The profile of optimal controls u_1^* and u_2^* is plotted in Fig. 3. The TB prevention should be done intensively for almost 10 years and then decreasing in year 10. Meanwhile, the chemoprophylaxis for latent TB should be done intensively for the first 2.5 years and then decreasing.

Furthermore, the dynamics of latent TB in the child and adult populations are given in Fig. 4, and the dynamics of active TB in the child and adult populations are given in Fig. 5. Figs. 4(a)-4(b) show that TB prevention and chemoprophylaxis for latent TB controls provide a

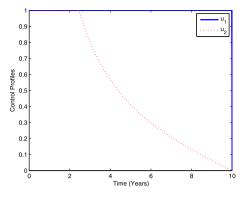


Fig. 3. Profile of optimal controls u_1^* and u_2^* .

significant reduction in latent TB in the child and adult populations compared to having no controls. Similar conditions also hold for active TB in the child and adult populations, i.e., active TB in both populations are lower compared to running the model without controls as depicted in Figs. 5(a)-5(b).

6.2. Second strategy

In the second strategy, the optimal controls for TB prevention (u_1^*) and TB treatment (u_3^*) are implemented. The profile of the optimal controls u_1^* and u_3^* is given in Fig. 6. Using this strategy, TB prevention should be done intensively for nearly 10 years. Meanwhile, TB treatment is at the upper bound of 100% and decreases gradually to lower bound in 10 years.

Figs. 7 and 8 provide the dynamics of latent TB infections in the child and adult populations as well as active TB in the child and adult populations, respectively, using the optimal controls u_1^* and u_3^* . This strategy provides a significant reduction in latent TB in the child and adult populations compared to the scenario without controls. Using this strategy, active TB in the child and adult populations decreases more than it would in the absence of controls.

6.3. Third strategy

In the third strategy, we implement the combination of optimal controls for chemoprophylaxis for latent TB (u_2^*) and TB treatment (u_3^*) for simulation. The profile of the optimal controls u_2^* and u_3^* is given in Fig. 9. Using this strategy, chemoprophylaxis for latent TB and TB treatment should be done intensively for almost 10 and 9.5 years, respectively, and then decreases to the lower bound.

Figs. 10 and 11 show the dynamics of latent TB and active TB in the child and adult populations, respectively, using the optimal controls u_2^* and u_3^* . In utilizing this strategy, we observe in Figs. 10(a)-10(b) that latent TB in both populations is less than the latent TB in both populations when no controls are used. Similarly, in Figs. 11(a)-11(b), we observed that active TB in both populations is lower when the control strategies are adopted than it is without controls.

6.4. Fourth strategy

In the last strategy, a combination of optimal controls for TB prevention (u_1^*) , chemoprophylaxis for latent TB (u_2^*) , and TB treatment (u_3^*) are implemented simultaneously. The profile of the optimal controls is given in Fig. 12. By using this strategy, TB prevention, chemoprophylaxis for latent TB, and TB treatment should be done intensively for almost 10, 2.3, and 1 years, respectively, and then decreased to the lower bound.

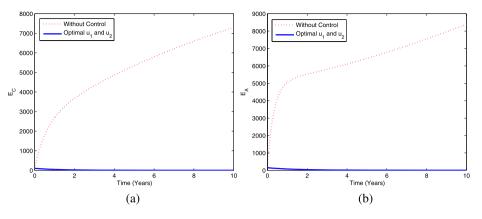


Fig. 4. The dynamics of latent TB in children (a) and adults (b) using controls u_1^* and u_2^* .

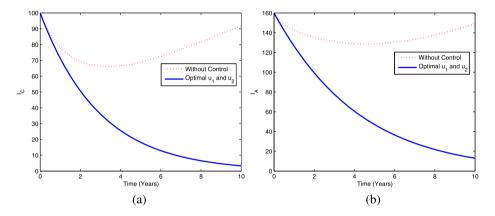


Fig. 5. Dynamics of active TB in children (a) and adults (b) using optimal controls u_1^* and u_2^* .

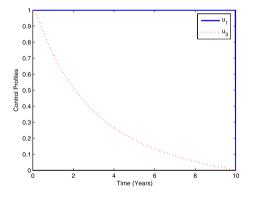


Fig. 6. Profile of optimal controls u_1^* and u_2^* .

Figs. 13 and 14 provide the dynamics of latent TB and active TB in the child and adult population, respectively, using the fourth strategy. The figures show that this optimal strategy provides a significant reduction in both latent TB and active TB in the child and adult population compared the scenario without controls.

Next, we compare the dynamics of models (1) and (2) (the singleand two-age-structured models) for the fourth strategy. First, we expand model (1) by incorporating TB prevention (u_1) for the susceptible population (*S*), chemoprophylaxis (u_2) for the latent TB population (*E*), and TB treatment (u_3) for the active TB population (*I*). The cost function is given by

$$J^{s}(u_{1}, u_{2}, u_{3}) = \int_{0}^{t_{f}} E + I + \frac{c_{1}}{2}u_{1}^{2} + \frac{c_{2}}{2}u_{2}^{2} + \frac{c_{3}}{2}u_{3}^{2}dt.$$
 (10)

The comparison between the dynamics for latent TB and active TB for the single- and two-age-structured models are shown in Fig. 15. The simulation results of Fig. 15(a) show that the total latent TB population for the two-age-structured model decreases more than the single-age model when using the fourth strategy. Similarly, Fig. 15(b) shows that the total active TB population in the two-age-structured model is less than that for the single-model using this set of controls. The significant reduction indicates that the two-age-structured model is better than the single-age model at controlling the spread of TB in the population.

The corresponding control profile for TB prevention (u_1) is displayed in Fig. 16, while the chemoprophylaxis (u_2) and TB treatment (u_3) are presented in Figs. 17(a) and 17(b), respectively. It can be seen from Fig. 16 that the efforts expended on TB prevention for the single- and two-age-structured models are not different. Moreover, from Fig. 17, we can see that the efforts expended on chemoprophylaxis and TB treatment for the single-age-structured model is greater than those expended for the two-age-structured model. The different efforts expended here are due to everyone in one-age-structured model is being treated using the adult rate.

7. Cost-effectiveness analysis

We could not easily determine the best optimal strategy due to the figures in Section 6 exhibiting similar patterns. Meanwhile, the third strategy performed the most poorly (see Figs. 10 and 11). Here, we conduct a cost-effectiveness analysis to determine the most effective strategy of the four strategies presented in Section 6.

To measure the differences between the costs and health outcomes of these four strategies, we use the incremental cost-effectiveness ratio (ICER) [37, 38, 39]. We use ratio ICER for comparing two intervention strategies that compete for the same resources. Ratio ICER could

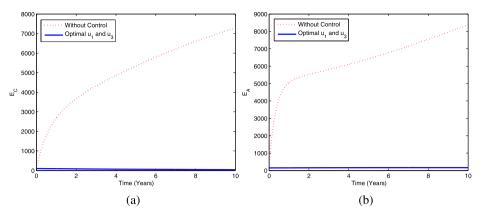


Fig. 7. The dynamics of latent TB in children (a) and adults (b) using optimal controls u_1^* and u_3^* .

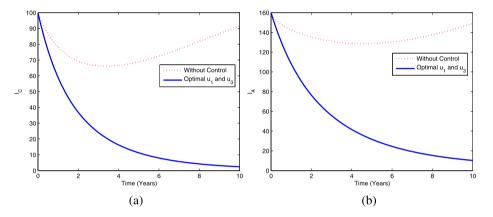


Fig. 8. The dynamics of active TB in children (a) and adults (b) using optimal controls u_1^* and u_3^* .

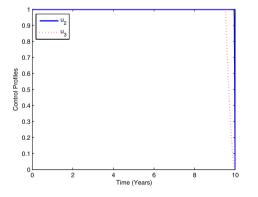


Fig. 9. Profile of optimal controls u_2^* and u_3^* .

be interpreted as the additional cost per additional health outcome. When measuring two or more competing strategies incrementally, one intervention should be compared with the next-less-effective alternative [40]. The ICER formula is as follows.

ICER =
$$\frac{\text{Difference in costs produced by strategies } i \text{ and } j}{\text{Difference in the total number of infection averted in strategies } i \text{ and } i}$$

The total number of averted infections is calculated from the difference between the total number of infected individuals without controls and the total infected individuals with controls. Moreover, for the total cost for the implemented strategies, we employed the cost functions, $\frac{c_1}{2}u_1^2, \frac{c_2}{2}u_2^2$, and $\frac{c_3}{2}u_3^2$ over time. We also used the parameter values in Table 3 to compute the total cost and total infections averted, as in Table 5, with an increasing order of total averted infections. The strategy to be excluded at each step is that corresponding to the highest ICER [41]. First, we compared the cost-effectiveness of strategies 1 and 2. The ICERs are calculated as follows.

$$ICER(1) = \frac{383.3547 - 0}{1.2399 \times 10^3 - 0} = 0.3092$$
$$ICER(2) = \frac{318.8270 - 383.3547}{1.4416 \times 10^3 - 1.2300 \times 10^3} = -0.3199.$$

From the values of ICER(1) and ICER(2), we can observe that strategy 2 is cheaper than strategy 1. In other words, strategy 1 is more costly and less effective than strategy 2. Therefore, strategy 1 is excluded from the set of options, and strategies 2 and 3 are compared.

ICER(2) =
$$\frac{318.8270}{1.4416 \times 10^3} = 0.2212$$

ICER(3) = $\frac{782.2304 - 318.8270}{1.6452 \times 10^3 - 1.4416 \times 10^3} = 2.2760$

Similarly, from the values of ICER(2) and ICER(3), it can be seen that strategy 2 is cheaper than strategy 3. Therefore, strategy 3 should be excluded from the set of options because strategy 3 is more costly and less effective than strategy 2. Hence, we continue on to the comparison of strategies 2 and 4.

$$ICER(2) = \frac{318.8270}{1.4416 \times 10^3} = 0.2212$$
$$ICER(4) = \frac{486.8425 - 318.8270}{1.7424 \times 10^3 - 1.4416 \times 10^3} = 0.5586.$$

Finally, from the values for ICER(2) and ICER(4), we can observe that strategy 2 is cheaper than strategy 4. Therefore, strategy 4 should

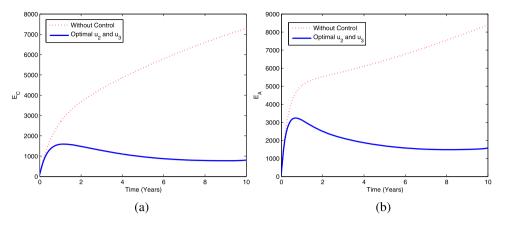


Fig. 10. The dynamics of latent TB in children (a) and adults (b) using optimal controls u_2^* and u_3^* .

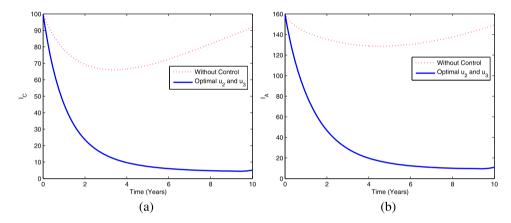


Fig. 11. The dynamics of active TB in children (a) and adults (b) using optimal controls u_2^* and u_3^* .

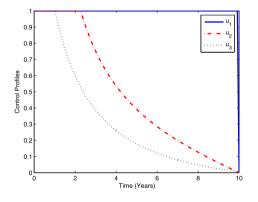


Fig. 12. Profile of optimal controls u_1^* , u_2^* and u_3^* .

be excluded from the set of options since it is more costly and less effective than strategy 2. Hence, we deduce that strategy 2 (the combination of TB prevention and TB treatment only) is the most cost-effective of all the strategies for TB control interventions.

Repeating the iteration process, we can decide the next most costeffective strategy. Thus, we arrive at strategy 4 being the next most cost-effective strategy after strategy 2, followed by strategy 1, then strategy 3. These findings indicate that strategy 3 is the least effective strategy.

8. Conclusion

In this paper, we constructed epidemic models of TB transmission within single- and two-age-structured populations. From the analysis of the models, we got the basic reproduction ratios that determine the existence and local stability of the equilibria. If the ratios are less than unity, then the disease-free equilibriums are locally asymptotically stable. On the contrary, the disease will endemic in the population whenever the ratios are greater than unity. We also compared the sensitivity indices of the basic reproduction ratios with respect to the parameters of the single- and the two-age-structured models. Finally, we extended the TB transmission model for an age-structured population by applying optimal control strategies.

We simulated the optimal control system by comparing with the system without control. The numerical simulations indicated that control strategies have a significant impact in terms of reducing TB infections in the population. However, the combination of chemoprophylaxis for latent TB and TB treatment has the least impact on TB infection reduction.

From the comparison results for the application of three control variables, it is shown that the total latent and infected populations for the two-age-structured model decreased more than they did in the singleage model. Thus, the effort expended for chemoprophylaxis for latent TB and TB treatment for two-age-structured model is less than that expended for the single model. The greater effort needed in single-agestructured population is due to all patients being managed via adult intervention.

Furthermore, we conducted ICER analysis for cost-effectiveness to deduce the most cost-effective control intervention. From the pairwise comparison results, we conclude that the combination of TB prevention and TB treatment is the most cost-effective strategy to implement. This is followed by the combination of three controls, the combination of TB prevention and chemoprophylaxis for latent TB, then the combination of chemoprophylaxis for latent TB and TB treatment.

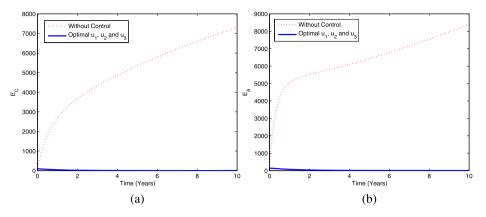


Fig. 13. The dynamics of latent TB in children (a) and adults (b) using optimal controls u_1^* , u_2^* and u_3^* .

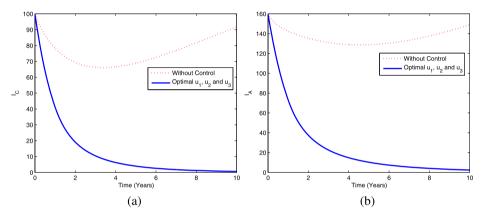


Fig. 14. The dynamics of active TB in children (a) and adults (b) using optimal controls u_1^* , u_2^* and u_3^* .

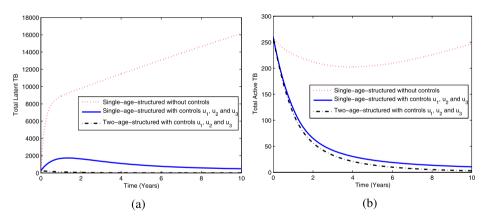


Fig. 15. The dynamics of total latent TB (a) and active TB (b) using optimal controls u_1^* , u_2^* and u_3^* .

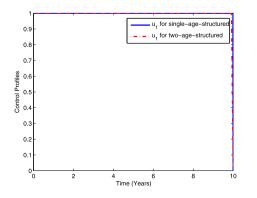


Fig. 16. The comparison of the control profiles u_1^* .

Declarations

Author contribution statement

Fatmawati, Hengki Tasman: Conceived and designed the experiments; Performed the experiments; Analyzed and interpreted the data; Wrote the paper.

Utami Dyah Purwati: Analyzed and interpreted the data. Firman Riyudha: Performed the experiments.

Funding statement

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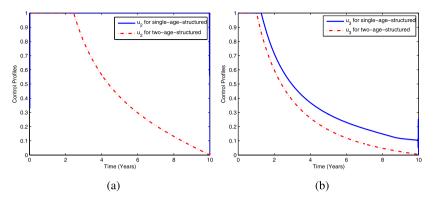


Fig. 17. The comparison of the control profiles u_2^* (a) and u_2^* (b).

Table 5

Number of averted infections and total cost of each strategy.

Strategy	Optimal controls	Total averted infection	Total cost
0	no controls	0	0
1	u_1^*, u_2^*	1.2399×10^{3}	383.3547
2	$u_1^{\hat{i}}, u_3^{\hat{i}}$	1.4416 ×10 ³	318.8270
3	u_{2}^{*}, u_{3}^{*}	1.6452×10^{3}	782.2304
4	$u_1^{\tilde{*}}, u_2^{\tilde{*}}, u_3^{*}$	1.7424 ×10 ³	486.8425

Competing interest statement

The authors declare no conflict of interest.

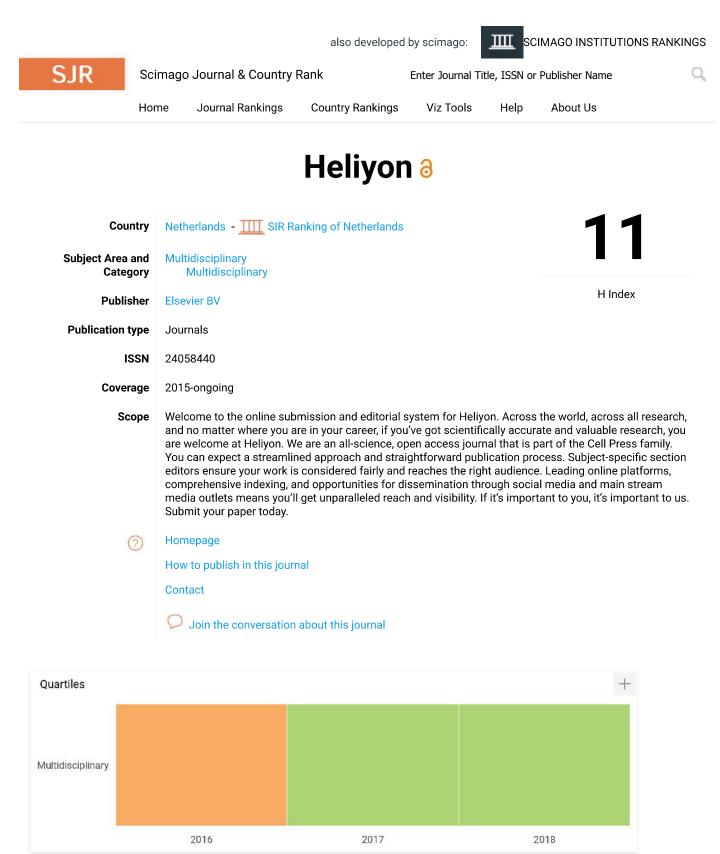
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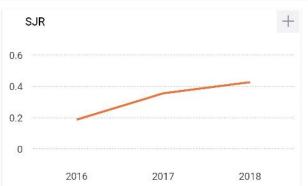
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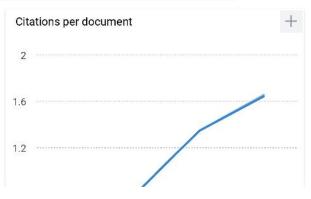
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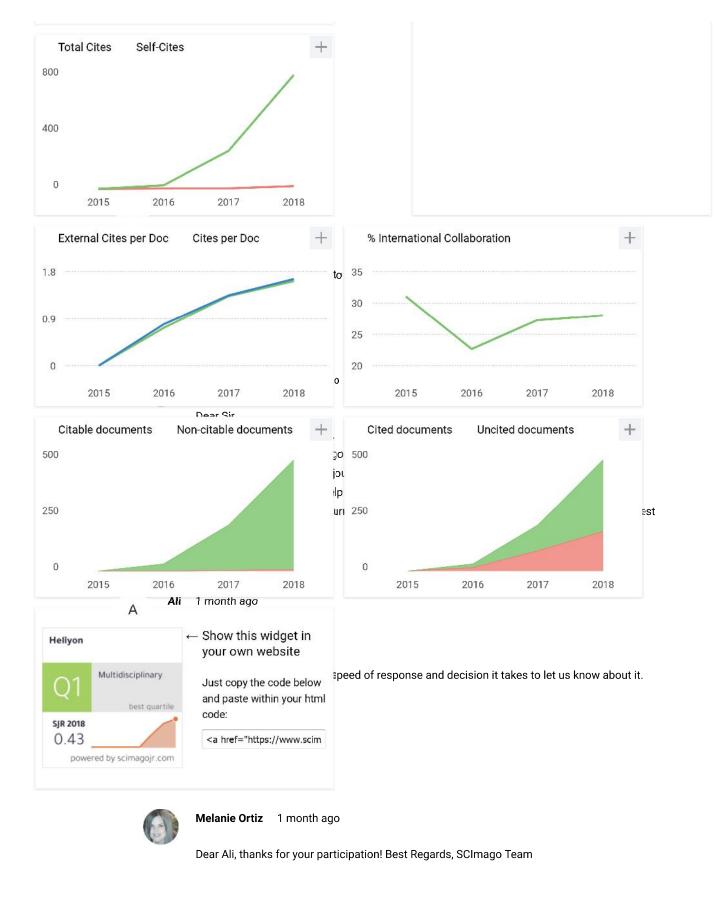
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