www.basic.ub.ac.id/conference Sici PROCEEDINGS **"Recent Advance in Basic Sciences Toward 4.0 Industrial Revolution**" March 20-21, 2019 **MIPA CENTER, Brawijaya University** Malang, Indonesia

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. Published under licence by IOP Publishing Ltd

PREFACE

Conference in a brief

The 9th Basic Science International Conference (BaSIC 2019) was a scientific meeting aimed to promote mutual exchange between scientists and experts, to exchange and share their experiences and research results on all aspects of basic science. The BaSIC 2019 also has provided a premier interdisciplinary platform for researchers, practitioners and educators to present and discuss the most recent innovations, trends, and concerns as well as practical challenges encountered and solutions adopted in the fields of basic sciences.

The conference was carried out with regards of the Rector of Brawijaya University's program to increase the number of publications of scientific paper in international journals or proceedings indexed by Scopus. Therefore, the selected full papers will be published in conference proceedings indexed by Scopus, IOP Conference Series: Materials Science and Engineering.

The conference has recorded **344 registered delegates** (presenters and nonpresenters), among which **350 participants** attended the conference. The participants consist of both international and national researchers, university lecturers, and college students in the field of basic sciences. In terms of country of origin, the participants of the BaSIC 2019 are coming from 7 countries, including Indonesia, Japan, Malaysia, Gambia, Libya, Saudi Arabia, and Thailand.

Plenary and Invited Speakers

- 1. Prof. Nikos Hadjichristidis (King Abdullah University of Science and Technology, Kingdom of Saudi Arabia)
- 2. Prof. Hideki Okamoto (Okayama University, Japan)
- 3. Prof. Roswanira Abdul Wahab (Malaysia University of Technology, Malaysia)
- 4. Dr Lakha Salaipeth (King Mongkut's University of Technology Thonburi, Thailand)
- 5. Dr Satria Zulkarnaen Bisri (RIKEN Center for Emergent Matter Science, JAPAN, Taiwan)
- 6. Dr rer nat Rino M Mukti (ITB, Indonesia)
- 7. Dr. Bagus Sartono (IPB, Indonesia)
- 8. Prof Moh Sasmito Djati (Universitas Brawijaya, Indonesia)

- 9. Dr Ani Budi Astuti (Universitas Brawijaya, Indonesia)
- 10. Dr Siti Mariyah Ulfa (Universitas Brawijaya, Indonesia)
- 11. Dr Noor Hidayat (Universitas Brawijaya, Australia)
- 12. Dr Zakiah Mohamed (Universitas Teknologi Mara, Malaysia)
- 13. Dr Sal Prima Yudha (Universitas Bengkulu, Indonesia)

9th Annual Basic Science International Conference 2019 (BaSIC 2019)

IOP Publishing

IOP Conf. Series: Materials Science and Engineering 546 (2019) 011001 doi:10.1088/1757-899X/546/1/011001

LIST OF COMMITTEE

Steering Committee

Rector

Dean of Faculty of Mathematics and Natural Sciences

Vice Dean I of Faculty of Mathematics and Natural Sciences

Vice Dean II of Faculty of Mathematics and Natural Sciences

Vice Dean III of Faculty of Mathematics and Natural Sciences

International Scientific Committee

Akhmad Sabarudin, D.Sc.

Brawijaya Unviersity, Indonesia

Prof. Widodo

Brawijaya University, Indonesia

Prof Hideki Okamoto

Okayama University, Japan

Prof James Ketudat-Cairns

Suranaree University of Technology, Thailand

Assoc. Prof. Roswanira Abdul Wahab

Malaysia University of Technology, Malaysia

Assoc. Prof. Francois Malherbe

Swinburne University of Technology, Australia

Organizing Committee

BaSIC 2019 Chair	: Anna Safitri, PhD
Secretary	: Indah Yanti, M. Si.
Finance	: Dr. Sc. Siti Mariyah Ulfa (Coordinator)
	Rustika Adiningrum, SE
Secretariat	: Sri Wardhani, M.Si. (Coordinator)
	Siti Mutrofin, M.Sc.
	Dewi Susanti, SE, MSA
	Muslikah, SE
Scientific Division	: Dr. Sc. Akhmad Sabarudin (coordinator)
	Dr. Rurini Retnowati
	Dr. rer. Nat Rahmat Triandi Tjahjanto
	Yuniar Ponco Prananto, M. Sc.
	Masruri, Ph.D

9th Annual Basic Science International Conference 2019 (BaSIC 2019)

IOP Conf. Series: Materials Science and Engineering **546** (2019) 011001 doi:10.1088/1757-899X/546/1/011001

IOP Publishing

	Zubaidah Ningsih, Ph.D
	Sri Herwiningsih, Ph.D
	Mauludi Ariesto Pamungkas, Ph.D
	Achmad Efendi, Ph.D
	Nurjannah, Ph.D
	Dian Siswanto, Ph.D
	Yoga Dwi Jatmiko, Ph.D
	Dr Isnani Darti
	Mila Kurniawaty, Ph.D
Program	: Dr. Arie Srihardyastutie (coordinator)
	Dr Ulfa Andayani
	M. Farid Rahman, M.Si.
Banquet	: Anna Roosdiana, M. App.Sc (coordinator)
	Ellya Indahyanti, M.Eng
	Ernawati Sukardi
Website and	: Dr. Sc. Lukman Hakim (coordinator)
Publication	Dimas Yusfrianto, S. Kom
	Hartoyo
Funding Division	: Prof Aulanni'am (coordinator)
	Dr Adam Wiryawan
Transportation	: Suratmo, M.Sc. (coordinator)
	Suliono
	Nurul Yakin
	Saiful Bahri
Logistics	: Danar Purwonugroho, M.Si (coordinator)
	Misbah Khunur, M.Si.
	Moh Amin SE
	Tri Wahyu Basuki, SE
	Djoema'ali, SE
	Widjianto, SE
	Agung Kurniawan
	Didik Siswanto
	Wasino
	Muh Hasan Muhajir, ST

PAPER • OPEN ACCESS

Peer review statement

To cite this article: 2019 IOP Conf. Ser.: Mater. Sci. Eng. 546 011002

View the article online for updates and enhancements.

Peer review statement

All papers published in this volume of *IOP Conference Series: Materials Science and Engineering* have been peer reviewed through processes administered by the proceedings Editors. Reviews were conducted by expert referees to the professional and scientific standards expected of a proceedings journal published by IOP Publishing.

This site uses cookies. By continuing to use this site you agree to our use of cookies. To find out more, see our Privacy and Cookies policy.

Table of contents

Volume 546

June 2019

Previous issue
 Next issue

View all abstracts

Papers		
OPEN ACCESS		052001
Modelling one-di	nensional crystal by using harmonic oscillator potential	
Abdurrouf, M. Nurh	uda and Wiyono	
➡ View abstract	🔁 PDF	
OPEN ACCESS		052002
The rule of radius	averaging in hydrogen atom	
Abdurrouf		
	🔁 PDF	
OPEN ACCESS		052003
Modelling of Hype	ertension Risk Factors Using Penalized Spline to Prevent Hypertension in Indonesia	
Tati Adiwati and Nu	r Chamidah	
➡ View abstract	🔁 PDF	
OPEN ACCESS		052004
Modeling of Parity Study: North Kalin	/ Status of The Mother and Basic Immunization Giving to Infants with Semiparametric Bivariate Probit (Case nantan Province in 2017)	
Rahmi Amelia, Muł	nammad Mashuri and M.Si Vita Ratnasari	
	🔁 PDF	
OPEN ACCESS		052005
Grey Wolf Optimiz	er for Parameter Estimation of Enzymatic Reaction in Biodiesel Synthesis	
Syaiful Anam and I	ndira Kumaralalita	
	PDF	
OPEN ACCESS		052006
Parameters Estim Crossover Operat	ation of Enzymatic Reaction Model for Biodiesel Synthesis by Using Real Coded Genetic Algorithm with Some ions	
Syaiful Anam		
	🔁 PDF	
OPEN ACCESS		052007
Quantitative risk r	nodelling of occupational safety in green-port	
Debrina Puspita An	driani, Vina Dwi Novianti, Rheza Adnandy and Qurrota A'yunin	
	PDF	
OPEN ACCESS		052008
Hybrid radial basi	s function with firefly algorithm and simulated annealing for detection of high cholesterol through iris images	
A Anjarsari, A Dama	ayanti, A B Pratiwi and E Winarko	
➡ View abstract	🔁 PDF	
OPEN ACCESS		052009

Analysis on Chronic Kidney Disease (CKD) Zuherman Rustam, Mas Andam Syarifah and Titin Siswantining + View abstract PDF	
OPEN ACCESS Geographically Weighted Regression in Cox Survival Analysis for Weibull Distributed Data with Bayesian Approach Ahmad Taufiq, Ani Budi Astuti and Adji Achmad Rinaldo Fernandes + View abstract PDF	052078
OPEN ACCESS Modeling of HIV and AIDS in Indonesia Using Bivariate Negative Binomial Regression Amin Tohari, Nur Chamidah and Fatmawati + View abstract PDF	052079
OPEN ACCESS Forecasting the Amount of Pneumonia Patients in Jakarta with Weighted High Order Fuzzy Time Series Sebastian Tricahya and Zuherman Rustam + View abstract PDF	052080
OPEN ACCESS Stability Analysis and Optimal Control of Lung Cancer Growth Model with Education Trisilowati + View abstract PDF	052081
OPEN ACCESS Interval Parameter Estimation of Quantile Regression Using Bca-Bootstrap Approach with Application to Open Unemployment Rate Study Solehatul Ummah, Vita Ratnasari and Dedy Dwi Prastyo + View abstract PDF	052082
OPEN ACCESS Non-monoton Nonparametric Variogram to Model the Land Price of Manado City with Hole Effect Periodicity Structure Winsy Weku, Henny Pramoedyo, Agus Widodo and Rahma Fitriani + View abstract PDF	052083
OPEN ACCESS Food Security of Farmer Households in The Papua Border Region In The Era of Industrial Revolution 4.0: Ordinal Logit Regression Model Agatha W. Widati, Dwidjono H. Darwanto, Masyhuri and Lestari R. Waluyati + View abstract PDF	052084
OPEN ACCESS A Maize Foliar Disease Mathematical Model with Standard Incidence Rate Windarto, Fatmawati and Kamara Mustiko Putri + View abstract PDF	052085
OPEN ACCESS A Mathematical Model of Social Media Popularity with Standard Incidence Rate Windarto, Utami Dyah Purwati and Nadiyah Amalia + View abstract M PDF	052086
OPEN ACCESS Development of Balmer Series Experiment Simulator in Mobile and Android Applications Firdy Yuana, Sugeng Rianto and Achmad Hidayat + View abstract PDF	052087
OPEN ACCESS Modeling and Simulation of Top and Bottom Lid Driven Cavity using Lattice Boltzmann Method K A Yuana, E P Budiana, Deendarlianto and Indarto	052088

+ View abstract 🔁 PDF	
OPEN ACCESS	052089
Soft Tissue Tumor Classification using Stochastic Support Vector Machine	
Durrabida Zahras, Zuherman Rustam and Devvi Sarwinda	
+ View abstract 🔁 PDF	
JOURNAL LINKS	
Journal home	
Information for organizers	
Information for authors	
Search for published proceedings	
Contact us	
Reprint services from Curran Associates	

PAPER • OPEN ACCESS

A Maize Foliar Disease Mathematical Model with Standard Incidence Rate

To cite this article: Windarto et al 2019 IOP Conf. Ser.: Mater. Sci. Eng. 546 052085

View the article online for updates and enhancements.



IOP ebooks[™]

Bringing you innovative digital publishing with leading voices to create your essential collection of books in STEM research.

Start exploring the collection - download the first chapter of every title for free.

A Maize Foliar Disease Mathematical Model with Standard **Incidence Rate**

Windarto^{1*}, Fatmawati¹, and Kamara Mustiko Putri¹

¹Department of Mathematics, Faculty of Science and Technology, Universitas Airlangga, Indonesia

Corresponding author e-mail: windarto@fst.unair.ac.id

Abstract. In this paper, we present a mathematical model of maize foliar disease with standard incidence rate. The present model is an improvement model from Collins and Duffy, where Collins and Duffy consider a mathematical model with the bilinear incidence rate. The present model has two equilibria namely the disease-free equilibrium and endemic equilibrium. We find that the disease-free equilibrium is asymptotically stable whenever the basic reproductive ratio is less than one. On the other hand, the endemic equilibrium will exist and be asymptotically stable whenever the basic reproductive ratio is greater than one. Furthermore, we perform numerical simulations to confirm the analytical results.

1. Introduction

Maize or corn (Zea mays L.) is one type of food crop planted by farmers. Maize is also one of staple foods in several regions in Indonesia. The main producing areas of corn in Indonesia are West Java, Central Java, East Java, Yogyakarta, Madura, East Nusa Tenggara, North Sulawesi, South Sulawesi and Maluku. Maize is classified in *Plantae* kingdom, *Spermatophyta* phylum, *Angiospermae* subphylum, Monocotyledonae class, Cyperales order, Poaceae family, Zea genus, Zea mays species [1].

During one life cycle of maize plants, every part of maize is vulnerable to a number of plant diseases. The diseases can reduce the quantity and quality of maize crop yields [2]. Maize diseases could be classified into bacterial diseases, fungal diseases, nematodes/parasitic diseases, virus diseases and viruslike diseases [3]. One of fungal diseases infects maize crop is Northern corn leaf blight. This disease is caused by Exserohilum turcicum / Helminthosporium turcicum species [4]. Damage to the maize leaf area during grain filling could cause a forty percent reduction in grain yield ([5], [6], and [7]).

Mathematical modelling has significant role in understanding many real problems, including infectious diseases spreading and plant diseases spreading. Suitable mathematical models can be used to analyse the dynamics of plant diseases. Many mathematical models have been constructed and analysed to describe the dynamics of plant disease transmission. Holt et al. developed a mathematical model of African mosaic virus diseases spread. The model from Holt et al. was a host-vector model, where the model contained four compartment, namely healthy cassava, infected cassava, non-infective whitefly vectors and infective whitefly vectors [8]. Jeger et al. also developed a host-vector model for describing plant-virus transmission. Jeger et al. applied a SEIR-type and SEI-type model to analyse the dynamics of host plant population and the dynamics of insect vector population respectively [9]. Jeger et al. improved their previous model to study the interactions between host plant, virus-plant and insect as vector of the virus [10]. Jeger et al. also applied a SIR-type mathematical model to explain direct transmission of plant virus through vector mating [11]. Meng and Li investigated effect of replanting of

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. Published under licence by IOP Publishing Ltd 1

healthy plants and removal of infected plants as treatments to control plant diseases spreading through a mathematical model [12].

Some researchers also investigated dynamics of maize diseases through mathematical models. Stewart el al. performed a mathematical simulation of *Fusarium* growth in maize ears after artificial inoculation [13]. Paul and Munkvold used regression technique and artificial neural network for the Prediction of gray leaf spot of maize [14]. Collins and Duffy formulated a mathematical model to study the impacts of maize foliar diseases on maize population [15].

In their model, Collins and Duffy studied the dynamics of susceptible plant, infected plant and pathogen dynamics. Collins and Duffy applied bilinear incidence rate to model reduction rate of susceptible maize due to pathogen infections. Bilinear incidence rate is only accurate in the early phases of an epidemic in a population of medium size ([16], [17]). In this paper, we improve the model from Collins and Duffy by consider standard incidence rate. In the next section, we present a mathematical model of maize foliar model with standard/fractional incidence rate. Then we discuss linear stability of equilibria of the proposed model. Then, we perform numerical simulations to illustrate analytical results of this study. Finally, conclusions of this study are presented in the last section.

2. The proposed model

In this section, we proposed a mathematical model of maize foliar disease spread. The proposed model is an improvement of the model from Collins and Duffy [15]. Here, we consider standard incidence rate to explain infection rate of pathogen to susceptible plants. The model was constructed under the following assumptions:

- (1) The model consists of three compartments, namely number of susceptible maize population (S), number of infected maize population (I) and number of pathogens population (P).
- (2) Susceptible maize populations are planted with constant rate.
- (3) Natural death rate of maize population is constant.
- (4) Death rate of infected maize plants due to pathogenic infection is constant.
- (5) The infection rate of susceptible maize by pathogen is constant.
- (6) The increasing rate of pathogen population is proportional to the number of infected maize population.
- (7) Death rate of pathogen population is constant.

Transmission diagram of the proposed model is presented in Figure 1.



Figure 1. Transmission diagram of maize foliar disease mathematical model.

From the assumptions, the dynamics of maize foliar disease could be described by the following differential equation system:

$$\frac{dS}{dt} = K - \frac{\beta SP}{S+I} - \mu S,\tag{1}$$

$$\frac{dI}{dt} = \frac{\beta SP}{S+I} - (\mu + \delta)I,$$
(2)

$$\frac{dF}{dt} = \sigma I - \varepsilon P. \tag{3}$$

The region of biological interest of the model in Eq. (1)-(3) is

 $\Omega \coloneqq \{ (S, I, P) \in R^3, S, I, P \ge 0, S + I > 0 \}.$ (4)

All parameters in the model in Eq. (1) - (3) are positive. When the number maize population is constant, the mathematical model with standard incidence rate in eq. (1)-(3) could be simplified into the model with bilinear incidence rate. Hence, the mathematical model with standard incidence rate could be considered as a generalization and an improvement of the model with bilinear incidence rate. Description of the parameters is presented in Table 1.

Table 1. Description of parameters of the proposed model	
Parameter	Description
К	Planted rate of susceptible maize
β	Infection rate of susceptible maize by pathogen
μ	Natural death rate of maize population
δ	Death rate of infected maize plants due to pathogenic infection
σ	Increasing/growth rate of pathogen population
3	Death rate of pathogen population

The differential equation (1) describes the dynamics of susceptible maize population. Susceptible maize population increases because of corn planting corn, and it decreases because of pathogen infection and natural death. The differential equation (2) shows the dynamics of infected maize population. Infected maize population increases due to infection of susceptible maize population by pathogen. On the other hand, infected maize population decreases due to natural deaths and pathogenic infection death. Equation (3) explains the pathogen population dynamics. Pathogen population increases due to the proliferation of pathogens in infected maize populations. On the other hand, pathogen population decreases due to natural death.

3. Analysis of the proposed model

The model in Eq. (1)-(3) has two equilibria, namely pathogen-free equilibrium (E_1) and pathogen equilibrium (E_2). The pathogen-free equilibrium is given by

$$E_1 := (S_1, I_1, P_1) = \left(\frac{\kappa}{\mu}, 0, 0\right).$$
(5)

The pathogen equilibrium is given by

$$\coloneqq (S_2, I_2, P_2) = \left(\frac{\kappa\varepsilon}{(\beta\sigma - \delta\varepsilon)}, \frac{\kappa\varepsilon(R-1)}{(\beta\sigma - \delta\varepsilon)}, \frac{\kappa\sigma(R-1)}{(\beta\sigma - \delta\varepsilon)}\right), \tag{6}$$

where

 E_2

$$R = \frac{\beta\sigma}{(\mu+\delta)\varepsilon}.$$
(7)

The pathogen-free equilibrium always exists. The pathogen equilibrium exists if and only if the threshold parameter R > 1. Here the threshold parameter R in eq. (7) is basic reproductive ratio of the proposed model in eq. (1)-(3).

The Jacobian matrix of the proposed model in Eq. (1)-(3) is given by

$$J = \begin{bmatrix} -\frac{\beta P}{S+I} + \frac{\beta S P}{(S+I)^2} - \mu & \frac{\beta S P}{(S+I)^2} & -\frac{\beta S}{S+I} \\ \frac{\beta P}{S+I} - \frac{\beta S P}{(S+I)^2} & -\frac{\beta S P}{(S+I)^2} - (\mu + \delta) & \frac{\beta S}{S+I} \\ 0 & \sigma & -\varepsilon \end{bmatrix}.$$
(8)

Stability of the pathogen-free equilibrium is presented in Theorem 1.

(10)

IOP Conf. Series: Materials Science and Engineering 546 (2019) 052085 doi:10.1088/1757-899X/546/5/052085

Theorem 1. The pathogen-free equilibrium E_1 is locally asymptotically stable if the basic reproductive ration is less than one. Moreover, the pathogen-free equilibrium is unstable if the basic reproductive ratio is greater than one.

Proof. The Jacobian matrix of the proposed model in eq. (1)-(3) evaluated at the pathogen-free equilibrium E_1 is given by

$$J(E_1) = \begin{bmatrix} -\mu & 0 & -\beta \\ 0 & -(\mu+\delta) & \beta \\ 0 & \sigma & -\varepsilon \end{bmatrix}.$$
(9)

Eigenvalues of $J(E_1)$ are obtained from the following characteristic polynomial $(\lambda + \mu)(\lambda^2 + (\mu + \delta + \varepsilon)\lambda + (\mu + \delta)\varepsilon - \beta\sigma)$

$$(\lambda + \mu)(\lambda^2 + (\mu + o + \varepsilon)\lambda + (\mu + o)\varepsilon - \beta\sigma) = 0$$

Hence eigenvalues of $J(E_1)$ are $\lambda_1 = -\mu$ and the zeros of the following quadratic polynomial $(\lambda^2 + (\mu + \delta + \varepsilon)\lambda + (\mu + \delta)\varepsilon - \beta\sigma) = 0.$

By using the Routh-Hurwitz theorem, all eigenvalues of $J(E_1)$ are negative or complex eigenvalues with negative real parts if and only if $R = \frac{\beta\sigma}{(\mu+\delta)\varepsilon} < 1$. Therefore, the pathogen-free equilibrium is locally asymptotically stable if the basic reproductive ratio is less than one.

If the basic reproductive ratio is greater than one, then the characteristic polynomial in eq. (10) has one positive roots. Hence, the Jacobian matrix $I(E_1)$ has one positive eigenvalue. Consequently, the pathogen-free equilibrium is unstable. This completes the proof.

Global stability of the pathogen-free equilibrium is presented in Theorem 2.

Theorem 2. If the basic reproductive ratio is equal or less than one, then the pathogen-free equilibrium E_1 is globally asymptotically stable.

Proof. We define a Lyapunov function

 $U: \{(S, I, P) \in \Omega : S > 0\} \rightarrow R$ where $U(S, I, P) = I + \frac{\beta}{s}P$.

U is a nonnegative function on the domain Ω . Moreover, U attains minimum value when I = P = 0. The time derivative of U evaluated at the solution of mathematical model in eq. (1)-(3) is given by

$$\frac{dU}{dt} = \frac{dI}{dt} + \frac{\beta}{\varepsilon} \frac{dP}{dt} = -\frac{\beta IP}{S+I} - \left[(\mu + \delta) - \frac{\beta \sigma}{\varepsilon} \right] I = -\frac{\beta IP}{S+I} - (\mu + \delta) [1 - R] I \le 0.$$

In addition, we find $\frac{dU}{dt} = 0$ if and only if I = 0 or P = 0. Hence, $I(t) \to 0$ or $P(t) \to 0$ as $t \to \infty$. From eq. (3), I(t) = 0 causes $P(t) \to 0$ as $t \to \infty$. Then by using P(t) = 0 in eq. (1), we find $S(t) \to \frac{K}{\mu}$ as $t \to \infty$.

Moreover, by using P(t) = 0 in eq. (1), we find $S(t) \to \frac{K}{\mu}$ as $t \to \infty$. We also find $I(t) \to 0$ as $t \to \infty$. ∞ whenever P(t) = 0. As a result, by using LaSalle invariant principle, we find that every solution of the mathematical model in eq.(1)-(3) with initial value in Ω tends to the pathogen-free equilibrium as $t \to \infty$ [18] \blacksquare .

Stability of pathogen equilibrium is presented in Theorem 3.

Theorem 3. The pathogen equilibrium E_2 is locally asymptotically stable whenever the basic reproductive ratio is greater than one.

Proof. Let $J(E_2)$ be the Jacobian matrix of the proposed model in eq. (1)-(3) evaluated at the pathogen equilibrium E₂. Eigenvalues of $J(E_2)$ satisfies the following characteristic polynomial

$$\lambda^3 + a_1\lambda^2 + a_2\lambda + a_3 = 0,$$

where

$$a_{1} = \frac{(R-1)\beta\sigma}{R\varepsilon} + 2\mu + \delta + \varepsilon = \frac{\beta\sigma}{\varepsilon} + \mu + \delta + \varepsilon,$$

$$a_{2} = \frac{\beta\sigma\mu R(R-1) + \beta\sigma\delta(R-1)^{2} + \beta\sigma\varepsilon(R-1)}{R^{2}\varepsilon} + \mu(\mu + \delta + \varepsilon),$$

$$a_{3} = \frac{\beta\sigma\mu(R-1) + \beta\sigma\delta(R-1)^{2}}{R^{2}}.$$

It is clear that $a_1, a_2, a_3 > 0$ whenever R > 1. By direct calculation we find that

IOP Publishing

$$\begin{aligned} a_1 a_2 - a_3 &= \frac{\beta \sigma \mu (R-1)^2 + \beta \sigma \varepsilon (R-1)}{R^2} + \left(\frac{\beta \sigma}{\varepsilon} + \mu + \delta + \varepsilon\right) \mu (\mu + \delta + \varepsilon) \\ &+ \left(\frac{\beta \sigma}{\varepsilon} + \mu + \delta\right) \left(\frac{\beta \sigma \mu R (R-1) + \beta \sigma \delta (R-1)^2 + \beta \sigma \varepsilon (R-1)}{R^2 \varepsilon}\right) > 0 \end{aligned}$$

By using the Routh-Hurwitz theorem, all eigenvalues of $J(E_2)$ are negative or complex eigenvalues with negative real parts if R > 1. As a result, the pathogen equilibrium is locally asymptotically stable if R > 1. This completes the proof.

4. Numerical Simulations

In this section, we present some numerical simulations to describe solution of the proposed model at pathogen-free condition and pathogen condition. Initial conditions of pathogen-free simulation are S(0) = 200, I(0) = 400, P(0) = 400. Some type of hybrid maize could be harvested after 97 days. Hence, we choose natural death parameter value $\mu = \frac{1}{97 \text{ day}} = 0.0103/\text{ day}$. Here we simulate the proposed model from t = 0 until t = 200 days. Parameter values used in the simulation are shown in Table 2.

Table 2. Parameter values used in the simulation

Parameter	Value	Source
K	10 plants / day	Assumption
β	0.1 / (pathogen . day)	Assumption
μ	0.0103 / day	Assumption
δ	0.0206 / day	Assumption
σ	0.0143 / day	[15]
3	0.1236 / day	[15]

From Table 2, we find the basic reproductive ratio R is R = 0.3744. In this condition, pathogen growth and the infection rate is lower than the pathogen removal rate (ϵ) and the infectious removal rate (μ + δ). This condition yields the pathogen-free condition. Consequently, infectious maize population and pathogen population tend to zero for enough long time. This situation is illustrated by the simulation result of pathogen-free condition (see the Figure 2).

We also perform numerical simulation for the pathogen condition. Parameter values for this simulation are shown in Table 2 except for parameter β . Here we choose $\beta = 0.5$. Hence we find the basic reproductive ration R is R = 1.8721. In this condition, pathogen growth and the infection rate is greater than the pathogen removal rate (ϵ) and the infectious removal rate ($\mu+\delta$). This condition yields the persistence of pathogen condition. Consequently, infectious maize population and pathogen population are always persist in the system. In addition, infectious maize population and pathogen population tend to the pathogen equilibrium values for enough long time. This situation is illustrated by the simulation result of pathogen condition (see the Figure 3).

5



Figure 2. Dynamics of maize disease spread mathematical model for pathogen-free condition



Figure 3. Dynamics of maize disease spread mathematical model for pathogen condition

5. Conclusion

In this paper, we have discussed a mathematical model of maize foliar disease spread with standard incidence rate. The proposed model has two equilibria, namely pathogen-free equilibrium and pathogen equilibrium. We found that property of the proposed model was completely determined by basic reproductive ration of the model.

Acknowledgment

The authors would like to thank the Ministry of Research, Technology and Higher Education Republik Indonesia for supporting this research.

References

- [1] CABI 2019 Zea mays, In: Invasive Species Compendium (*CAB International*, Wallingford UK). Available online at www.cabi.org/isc/datasheet/57417#toPictures
- [2] Sudjono M S Penyakit Jagung dan Pengendaliannya, Balai Penelitian Tanaman Pangan Bogor (Text in Indonesian). Available online at http://balitsereal.litbang.pertanian.go.id/wpcontent/uploads/2018/08/11penyakit.pdf
- [3] Hock J, Kranz J and Renfro B L 1995 Studies on the epidemiology of the tar spot disease complex of maize in Mexico, *Plant Pathology* 44(3) pp. 490-502.
- [4] Munkvold G P 2017, Diseases of Corn (syn. Maize) (*Zea mays* L.), *The American Phytopathological Society*. Available online at https://www.apsnet.org/publications/commonnames/Pages/Corn.aspx
- [5] Ferguson L M and Carson M L 2007 Temporal variation in Setosphaeria turcica between 1974 and 1994 and origin of races 1, 23, and 23N in the United States, *Phytopathology 97*(11) pp. 1501-1511.
- [6] Wang H, Xiao Z X, Wang F G, Xiao Y N, Zhao Jr R, Zheng Y L and Qiu F Z, 2012, Mapping of HtNB, a gene conferring nonlesion resistance before heading to Exserohilum turcicum (Pass.), in a maize inbred line derived from the Indonesian variety Bramadi, *Genetics and Molecular Research* 11(3) pp. 2523-2533.
- [7] Ribeiro R M, do Amaral Jr A T, Pena G F, Vivas M, Kurosawa R N and Gonçalves L S A, 2016, History of northern corn leaf blight disease in the seventh cycle of recurrent selection of an UENF-14 popcorn population, *Acta Scientiarum* 38(4) pp. 447-455.
- [8] Holt J, Jeger M J, Thresh J M and Otim-Nape G W, 1997, An epidemiological model incorporating vector population dynamics applied to African cassava mosaic virus disease, *Journal of Applied Ecology* 34(3) pp. 793-806.
- [9] Jeger M J, van Den Bosch F, Madden L V and Holt J, 1998, A model for analysing plant-virus transmission characteristics and epidemic development, *IMA Journal of Mathematics Applied in Medicine and Biology* 15(1) pp. 1–18.
- [10] Jeger M J, Holt J, van den Bosch F and Madden L V, 2004, Epidemiology of insect-transmitted plant viruses: Modelling disease dynamics and control interventions, *Physiological Entomology* 29(3) pp. 291–304.
- [11] Jeger M J, Madden L V and van den Bosch F, 2009, The effect of transmission route on plant virus epidemic development and disease control, *Journal of Theoretical Biology* 258(2) pp. 198-207.
- [12] Meng X and Li Z, 2010, The dynamics of plant disease models with continuous and impulsive cultural control strategies, *Journal of Theoretical Biology* 266 pp. 24-40.
- [13] Stewart D W, Reid L M, Nicol R W and Schaafsma A W 2002, A Mathematical Simulation of Growth of *Fusarium* in Maize Ears After Artificial Inoculation, *Phytopathology* 92(5) pp. 534-541.
- [14] Paul P A and Munkvold G P 2005, Regression and Artificial Neural Network Modeling for the Prediction of Gray Leaf Spot of Maize, *Phytopathology* 95(4) pp. 388-396.
- [15] Collins O C and Duffy K J, 2016, Optimal control of maize foliar disease using the plants population dynamics, *Acta Agriculturae Scandinavica Section B – Soil & Plant Science* 66(1) pp. 20-26.
- [16] Brauer F and Castillo-Chaves C., 2011, Mathematical Models in Population Biology and Epidemiology Second Edition, *Springer*.
- [17] Windarto and Anggriani N, 2015, Global stability for a susceptible-infectious epidemic model with fractional incidence rate, *Applied Mathematical Sciences* 9(76) pp. 3775 3788.
- [18] LaSalle J P, 1976, The stability of dynamical systems (Philadelphia: SIAM).



IOP Conference Series: Materials Science and Engineering

Country	United Kingdom - IIII SIR Ranking of United Kingdom
Subject Area and Category	Engineering Engineering (miscellaneous)
	Materials Science (miscellaneous) H Index
Publisher	
Publication type	Conferences and Proceedings
ISSN	17578981, 1757899X
Coverage	2009-ongoing
Scope	The open access IOP Conference Series provides a fast, versatile and cost-effective proceedings publication service for your conference. Key publishing subject areas include: physics, materials science, environmental science, bioscience, engineering, computational science and mathematics.
0	Homepage
	How to publish in this journal
	Contact
	Ø Join the conversation about this journal







0

Ondrej 3 months ago

Madhu means if the journal is approved and listed in University Grants Commission of India. It is possible to find it out here (after registration):

https://ugccare.unipune.ac.in/site/website/index.aspx

However, IOP Conference Series: Materials Science and Engineering, is not, in fact, journal, but it collects proceedings from conferences, not journal articles. Still, the good thing is that IOP CS is WOS, Scopus (SJR) indexed. Generally, IOP publishing house is fair and reilable institution.



Melanie Ortiz 3 months ago

Dear user, thanks for your participation! Best Regards, SCImago Team



Melanie Ortiz 3 months ago

Dear Madhu, could you please expand your comment? Best Regards, SCImago Team