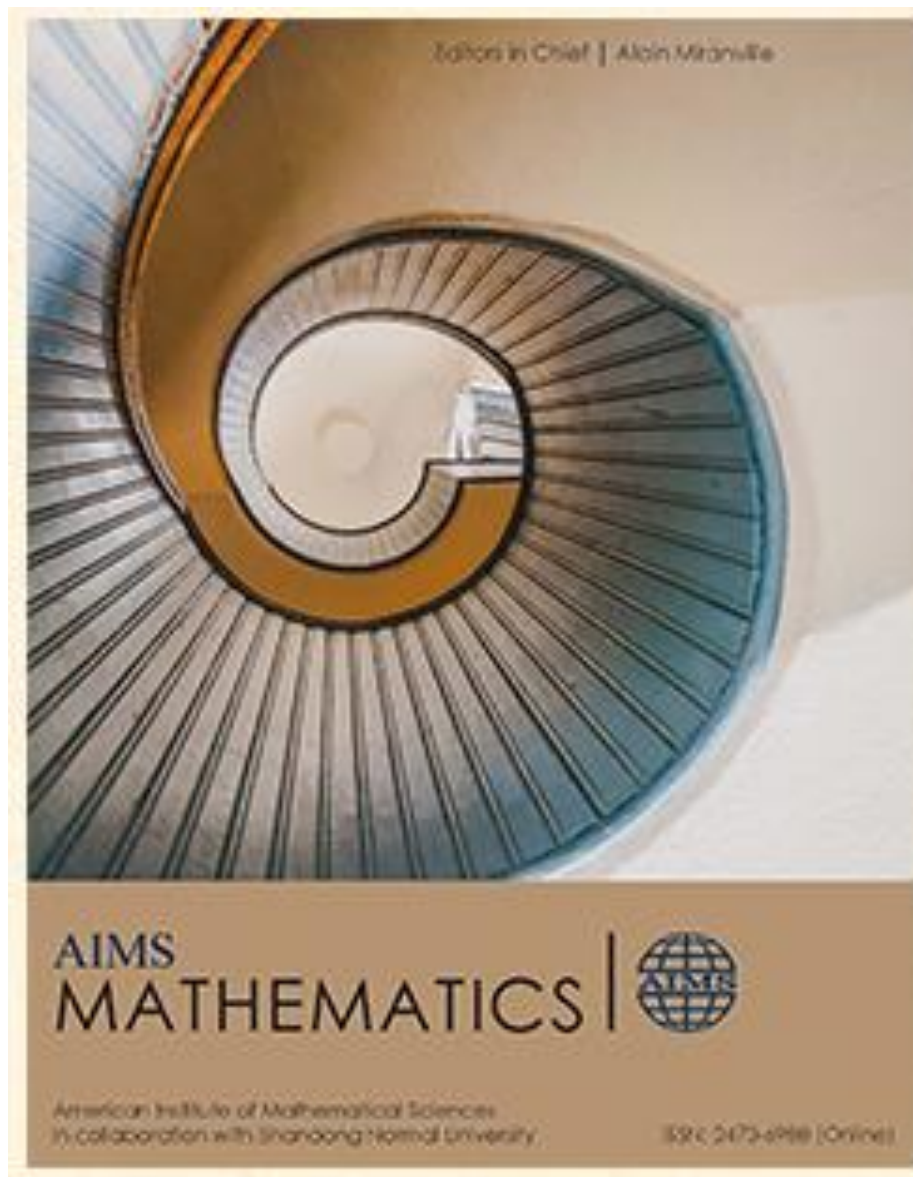


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Windarto, Muhammad Altaf Khan, Fatmawati

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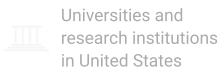
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Alain.Miranville@math.univ-poitiers.fr

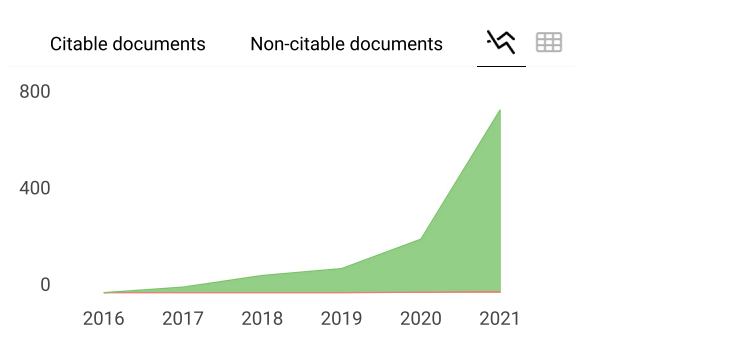
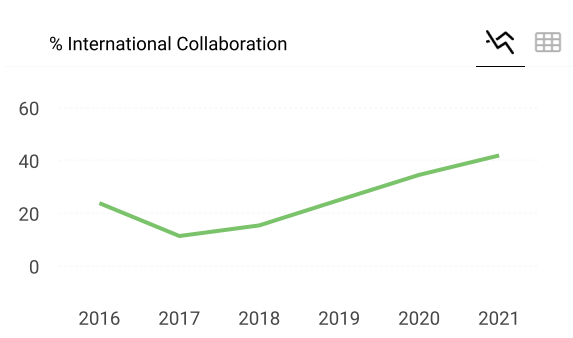
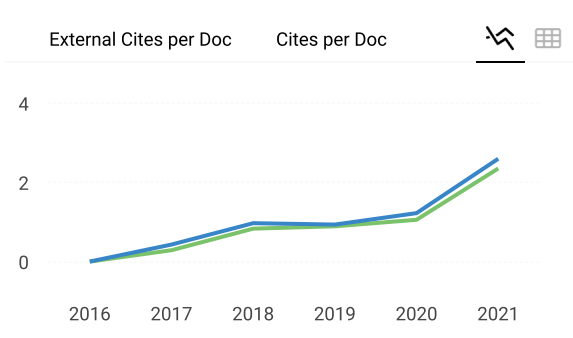
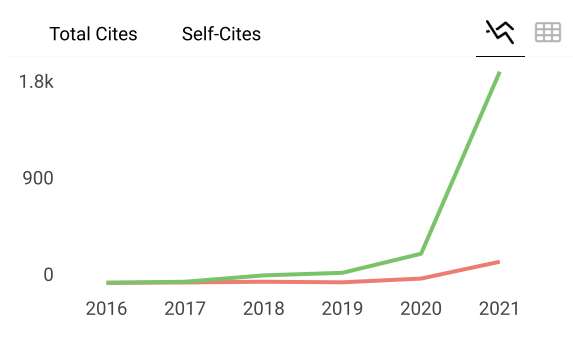
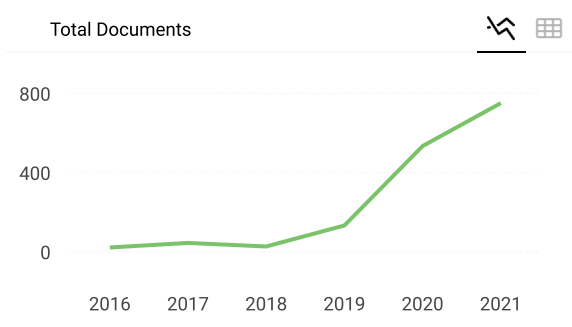
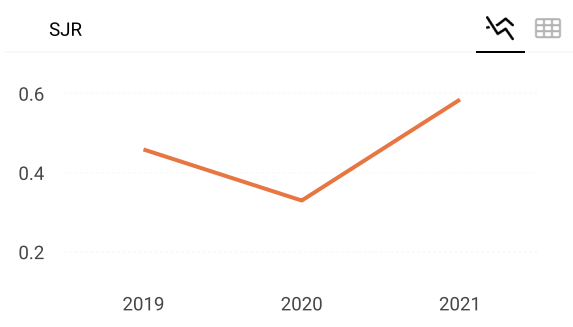
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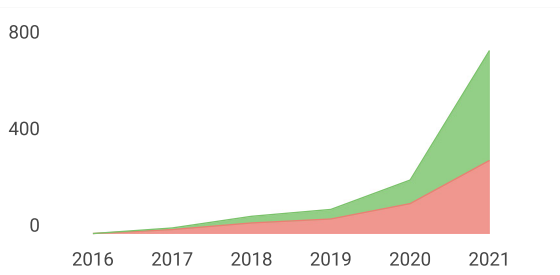
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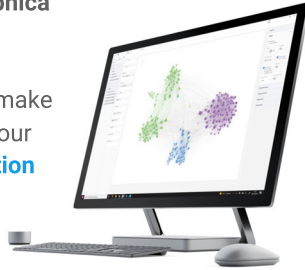
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Université de Poitiers, Laboratoire de Mathématiques et Applications, UMR CNRS 7348, SP2MI, 86962 Chasseneuil Futuroscope Cedex, France

Qing Miao (Managing Editor)



(mailto:mathematics@aimspress.org)

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Sectional editors:

Maria Alessandra Ragusa



(mailto:maragusa@dmi.unict.it)

Universita di Catania, Viale Andrea Doria, 6-95125 Catania, Italy
Differential Equations, Partial Differential Equations and Applied Mathematics

Antonio Di Crescenzo



(mailto:adicrescenzo@unisa.it)

Dipartimento di Matematica, Università degli Studi di Salerno, Italy
Probability and Statistics

Shaofang Hong



(mailto:sfhong@scu.edu.cn)

Mathematical College, Sichuan University, Chengdu 610064, P.R. China
Algebra and Number theory

Editors:

Toyohiko Aiki
✉ (mailto:aikit@fc.jwu.ac.jp)

Faculty of Science, Japan Women's University, Tokyo,
Japan
Free boundary problem and Hysteresis operator

Ricardo Almeida
✉ (mailto:ricardo.almeida@ua.pt)

Departamento de Matemática, Universidade de
Aveiro, Campus de Santiago 3810-193 Aveiro,
Portugal
*Fractional calculus, calculus of variations, optimal
control*

Luis J. Alías ✉ (mailto:ljalias@um.es)

Departamento de Matemáticas, Universidad de
Murcia, E-30100 Espinardo, Murcia, Spain
Differential Geometry and Geometric Analysis

Abdon Atangana
✉ (mailto:AtanganaA@ufs.ac.za)

Institute for Groundwater Studies, University of the
Free State, South Africa
*Fractional Calculus and Their Applications, Methods for
Partial Differential Equations*

Alicia Cordero Barbero
✉ (mailto:acordero@mat.upv.es)

D. Matemática Aplicada, E.T.S.I. de
Telecomunicación, Universitat Politècnica de
València, Camino de Vera, s/n, 46022-Valencia, Spain
*iterative methods for solving nonlinear problems, real
or complex discrete dynamical systems*

Pierre Bieliavsky
✉ (mailto:pierre.bieliavsky@uclouvain.be)

Institut de Recherche en Mathématique et en
Physique, Université catholique de Louvain, Louvain la
Neuve, Belgium.
Differential Geometry and Lie Theory

Stefano Bonaccorsi



(mailto:stefano.bonaccorsi@unitn.it)

Department of Mathematics, University of Trento, via Sommarive 14, 38123 Povo (Trento), Italy
Malliavin calculus and its applications to the study of stochastic differential equations in infinite dimensions, Stochastic evolution equations with inhomogeneous boundary conditions and applications to evolution equations on networks

Tomasz Brzezinski



(mailto:t.brzezinski@swansea.ac.uk)

Department of Mathematics, Swansea University, Swansea, U.K.

Noncommutative geometry, Hopf algebras

Jinde Cao



(mailto:jdcao@seu.edu.cn)

Southeast University, Nanjing 210996, Jiangsu, China

Complex networks and complex systems, Multi-agent systems, and Dynamics of neural networks

Tomás Caraballo



(mailto:caraball@us.es)

Departamento de Ecuaciones Diferenciales y Análisis Numérico. Facultad de Matemáticas, Universidad de Sevilla. Avenida Reina Mercedes s/n. 41012-Sevilla, Spain

Non-autonomous and Stochastic dynamical systems, Differential equations with delay and memory

Claudia Ceci



(mailto:c.ceci@unich.it)

Department of Economics, University "G. D'Annunzio" of Chieti-Pescara, Viale Pindaro, 42, I-65127 Pescara, Italy

Stochastic models in finance, Filtering and stochastic control

Jean-Paul Chehab



(mailto:jean-paul.chehab@u-picardie.fr)

Laboratoire LAMFA (UMR CNRS 7352), Université de Picardie Jules Verne, Pôle Scientifique, 33, rue Saint Leu, 80 039 Amiens Cedex 1, France

Numerical Analysis and Numerical Linear Algebra

- Yanping Chen
✉ (mailto:yanpingchen@scnu.edu.cn)
School of Mathematical Sciences South China Normal University, Guangzhou 510631, China
Mixed finite element methods, Numerical methods for miscible displacement problems, Moving mesh methods for singularly perturbed problems, Adaptive mixed FEM for optimal control problems, Numerical analysis of spectral methods
- Laurence Cherfils
✉ (mailto:laurence.cherfils@univ-lr.fr)
Université de La Rochelle, Avenue Michel Crépeau, 17042 La Rochelle cedex 1, France.
PDEs and Numerical analysis
- J. Alberto Conejero
✉ (mailto:aconejero@upv.es)
✉ (mailto:albertconejero@gmail.com)
Instituto Universitario de Matemática Pura y Aplicada. Universitat Politècnica de València, Spain
Chaotic dynamical systems, Fractional calculus, Network Science, Mathematical applications in Biology, Computer science, and Engineering
- Monica Conti
✉ (mailto:monica.conti@polimi.it)
Dipartimento di Matematica, Politecnico di Milano, Italy
Asymptotic behavior of dynamical systems , Equations with memory
- Luca Dede'
✉ (mailto:luca.dede@polimi.it)
MOX, Mathematics Department, Politecnico di Milano, Piazza Leonardo da Vinci 32, 20133 Milano, Italy
Research interest: Numerical analysis, Mathematical and numerical modeling of Partial Differential Equations, Scientific Computing
- Feiqi Deng
✉ (mailto:aufqdeng@scut.edu.cn)
South China University of Technology, China
Stabilization and control, Nonlinear and networked systems

Zengji Du

✉ (mailto:duzengji@163.com)

✉ (mailto:zjdu@jsnu.edu.cn)

Jiangsu Normal University, China

*Dynamical systems, Singular perturbation theory,
Mathematical biology*

Arnaud Ducrot

✉ (mailto:arnaud.ducrot@univ-lehavre.fr)

Université Le Havre Normandie, Le Havre, France

Differential Equations and Applications in Biology

Jean-François Dupuy

✉ (mailto:Jean-Francois.Dupuy@insa-rennes.fr)

Institut de Recherche Mathématiques de Rennes,
INSA de Rennes, 20 Avenue des Buttes de Coësmes,
CS 70839, 35708 Rennes cedex 7, France

Statistical modeling and Data analysis

Boualem Djehiche

✉ (mailto:boualem@kth.se)

Department of Mathematics, KTH Royal Institute of
Technology, S-100 44 Stockholm, Sweden

*Stochastic Analysis and include Stochastic Control and
Differential Games, Insurance Mathematics and
Mathematical Finance*

Alberto Facchini

✉ (mailto:facchini@math.unipd.it)

Dipartimento di Matematica, University of Padova,
Padova, Italy.

Module theory and Ring theory

Raúl M. Falcón

✉ (mailto:rafalgan@us.es)

Departamento de Matemática Aplicada I. Universidad
de Sevilla. Spain

Combinatorics, Algebraic Geometry

Zhaosheng Feng

✉
(mailto:zhaosheng.feng@utrgv.edu)

School of Mathematical and Statistical Sciences,
University of Texas-Rio Grande Valley, Edinburg, Texas
78539, USA

*lie in analysis on differential equations (odes and
pdes), mathematical physics and mathematical biology*

Anna Fino

✉ (mailto:annamaria.fino@unito.it)

Dipartimento di Matematica "G. Peano", Università di Torino, via Carlo Alberto 10, 10123 Torino, Italia
Differential Geometry and Complex Geometry

Emmanuel Frénod

✉ (mailto:emmanuel.frenod@univ-ubs.fr)

Emmanuel Frénod, Université Bretagne Sud & LMBA (UMR6205), Campus de Tohannic, 56000 Vannes, France
Asymptotic Analysis, Mathematical Modelling

José L. Galán-García

✉ (mailto:jlgalan@uma.es)

Departamento de Matemática Aplicada. Escuela de Ingenierías Industriales. Universidad de Málaga, Spain
Applications of Computer Algebra Systems; Mathematical programming; Mathematics Education

Stefania Gatti

✉ (mailto:stefania.gatti@unimore.it)

Dipartimento di Scienze Fisiche, Informatiche e Matematiche, Università degli Studi di Modena e Reggio Emilia, via Campi 213/B, Modena, Italy
Partial differential equations, Asymptotic behavior of dynamical systems associated with evolution equations of hyperbolic and parabolic type

Yuxin Ge

✉ (mailto:yge@math.univ-toulouse.fr)

Institut de Mathématiques de Toulouse, Université Paul Sabatier, 118, route de Narbonne, 31062 TOULOUSE Cedex 9, France
Geometric analysis and Elliptic PDE

Paolo Gibilisco

✉ (mailto:paolo.gibilisco@uniroma2.it)

Department of Economics and Finance, University of Rome "tor Vergata"
Information geometry and Uncertainty relations

Maurizio Grasselli



(mailto:maurizio.grasselli@polimi.it)

Dipartimento di Matematica, Politecnico di Milano,
Italy.

*Infinite-dimensional dissipative dynamical systems,
Phase field models*

Marcus Greferath

(mailto:marcus.greferath@aalto.fi)

Dept. Mathematics and Systems Analysis, Aalto
University School of Science, P.O. Box 11100, FI-00076
Aalto, Finland

*Algebra and Discrete Mathematics, Mathematics of
Communications*

Xiaoying Han

(mailto:xzh0003@auburn.edu)

Auburn University, USA

*Non-autonomous and random dynamical systems,
Stochastic differential equations and applications*

Jens Høyrup (mailto:jensh@ruc.dk)

Section for Philosophy and Science Studies, Roskilde
University, Denmark

*History of mathematics in pre- and early Modern
cultures , Interaction between cultures and between
scholarly and practitioners' mathematics*

Aziz Hamdouni

(mailto:ahamdoun@univ-lr.fr)

Université de La Rochelle, Avenue Michel Crépeau,
17042 La Rochelle cedex 1, France

Modelling and Fluid mechanics

Salvador Hernández

(mailto:hernande@mat.uji.es)

Departamento de Matematicas, Universitat Jaume I,
12071 Castellon, Spain

*Topological groups , Spaces and groups of continuous
functions*

Minvydas Kazys Ragulskis

(mailto:minvydas.ragulskis@ktu.lt)

Department of Mathematical Modelling, Kaunas
University of Technology, Studentu 50-146, Kaunas
LT-51368, Lithuania

*Mathematical Application in Biomedicine, Engineering;
Nonlinear Dynamics and Chaos; Nonlinear PDE*

Boualem Khouider
✉ (mailto:khouider@uvic.ca)

University of Victoria, Canada
Applied mathematics, Numerical analysis and PDEs

Syed N.U.A. Kirmani
✉ (mailto:syed.kirmani@uni.edu)

Department of Mathematics, University of Northern Iowa, Cedar Falls, Iowa 50614-0506, U.S.A.
Probability(applied probability and stochastic processes), Mathematical Statistics(applications to statistical machine learning and predictive analytics)

Igor Kukavica
✉ (mailto:ikukavica@gmail.com)

Department of Mathematics, University of Southern California, 3620 S. Vermont Ave., KAP 108, Los Angeles, CA 90089, USA
Fluid dynamics and Navier-Stokes equations

Leskelä Lasse
✉ (mailto:lasse.leskela@aalto.fi)

Aalto University School of Science Department of Mathematics and Systems Analysis Otakaari 1, 02015 Espoo, Finland
Applied probability, Random graphs and network statistics

Alberto Lastra
✉ (mailto:alberto.lastra@uah.es)

Departamento de Física y Matemáticas, Universidad de Alcalá, Spain
Complex ODEs, PDEs and q-difference equations. Formal and analytic solutions

Manue de Leon
✉ (mailto:mdeleon@icmat.es)

Instituto de Ciencias Matemáticas, CSIC, c/ Nicolás Cabrera 13-15, 28049 Madrid, Spain
Differential geometry and Symplectic geometry, Poisson manifolds

Ji Li
✉ (mailto:ji.li@mq.edu.au)


Department of Mathematics and Statistics, Macquarie University, NSW, 2109, Australia
Harmonic analysis, Operator theory

Xiaodi Li  (mailto:lxid@sdu.edu.cn)

School of Mathematics and Statistics, Shandong
Normal University Ji'nan, Shandong, China

Xiaohu Li
 (mailto:Xiaohu.Li@stevens.edu)


Department of Mathematical Sciences, Stevens
Institute of Technology, Hoboken NJ 07030, USA
*Statistics and applied probability, Financial and
actuarial risk*

Jia Liu  (mailto:jliu@uwf.edu)

Department of Mathematics and Statistic, University
of West Florida, Pensacola, USA
Iterative methods and Preconditioning techniques

Lei Liu  (mailto:liuleill@live.cn)



College of Science, Liaoning University of Technology,
Jinzhou, Liaoning, China
*Fuzzy control, Neural network control, and Active
suspension system*

Alfonso Suarez Llorens
 (mailto:alfonso.suarez@uca.es)

Departamento de Estadística e I. O. Universidad de
Cádiz, Facultad de Ciencias, Polígono Río San Pedro,
11510, Puerto Real, Cádiz, Spain
Risk Management and Reliability

Songting Luo
 (mailto:luos@iastate.edu)

Department of Mathematics, Iowa State University,
Ames, IA 50011, USA
*Numerical Analysis, Scientific Computing, Numerical
Partial Differential Equations*

Haifeng Ma
 (mailto:haifengma@aliyun.com)
 (mailto:hfengma@163.com)

Department of Mathematics, Harbin Normal
University, China
Linear algebra, matrix theory and operator theory

Kirill Mackenzie



(mailto:k.mackenzie@sheffield.ac.uk)

School of Mathematics and Statistics, University of Sheffield, Hicks Building, Hounsfield Road, Sheffield, S3 7RH, UK

Poisson geometry, Multiple lie theory

Pierre Magal



(mailto:pierre.magal@u-bordeaux.fr)

Institut de Mathématiques de Bordeaux, Université de Bordeaux, 351 cours de la libération 33400 Talence, France

Differential Equations, Dynamical Systems, and mathematical modeling; epidemiology; ecology modeling

Dumitru Motreanu



(mailto:motreanu@univ-perp.fr)

Department of Mathematics, University of Perpignan, Perpignan, France

Nonlinear elliptic problems and Variational methods

Juan J. Nieto



(mailto:juanjose.nieto.roig@usc.es)

Institute of Mathematics, University of Santiago de Compostela, 15782, Spain

Differential equations, Fractional calculus, Mathematical applications in biomedicine

Alfred G. Noël



(mailto:anoel@math.umb.edu)

Department of Mathematics. The University of Massachusetts at Boston 100 Morrissey Blvd. Boston, MA 02125-3393, USA

Representation Theory and Computational Lie Theory

Sotiris K. Ntouyas



(mailto:sntouyas@uoi.gr)

Department of Mathematics, University of Ioannina, 451 10 Ioannina, Greece

Initial and Boundary Value Problems for Differential Equations, Inequalities, Asymptotic behavior, Controllability

Tohru Ozawa

✉ (mailto:txozawa@waseda.jp)

Department of Applied Physics, Waseda University,
Tokyo 169-8555, Japan

*Nonlinear Schrodinger Equations, Nonlinear
Hyperbolic Equations, Function Spaces*

Morgan Pierre

✉ (mailto:morgan.pierre@math.univ-
poitiers.fr)

Université de Poitiers & CNRS, Téléport 2—BP 30179,
Boulevard Marie et Pierre Curie, 86962 Futuroscope
Chasseneuil Cedex, France

*Numerical analysis of phase transition models (Allen-
Cahn, Cahn-Hilliard and phase-field crystal type
equations), Optimization of ship hulls*

Alfred Peris

✉ (mailto:aperis@mat.upv.es)

Institut Universitari de Matemàtica Pura i
Aplicada, Universitat Politècnica de
València, València, SPAIN

Topological dynamics, Linear dynamics

Yuming Qin

✉ (mailto:yuming_qin@hotmail.com)

Donghua University, Shanghai, China

Fluid dynamics

Ramon Quintanilla

✉
(mailto:ramon.quintanilla@upc.edu)

Departament de Matemàtiques, ESEIAAT, Universitat
Politécnica de Catalunya (UPC), Colom 11, S-08222
Terrassa, Barcelona, Spain

*Classical and Non-classical Thermoelasticity, Spatial
and Time stability*

Vicentiu Radulescu

✉ (mailto:radulescu@inf.ucv.ro)

Institute of Mathematics "Simion Stoilow" of the
Romanian Academy, 21 Calea Grivitei, 010702
Bucharest, Romania

*Nonlinear elliptic partial differential equations,
Variational and topological methods*

Andrea Scapellato

✉ (mailto:andrea.scapellato@unict.it)

Dipartimento di Matematica e Informatica, Università degli Studi di Catania, Italy

Function Spaces, Ordinary and Partial Differential Equations, Variational and Topological Methods

Giulio Schimperna

✉ (mailto:giusch04@unipv.it)

Dipartimento di Matematica, Università di Pavia, Via Ferrata 1, I-27100 Pavia, Italy

Evolutionary PDEs, Phase transition and thermomechanical models

Óscar Valero Sierra

✉ (mailto:o.valero@uib.es)

Department of Mathematical and Information Sciences, Universidad de las Islas Baleares, Spain

Fixed Point Theory, Generalized Metric Structures

Cristiana J. Silva

✉ (mailto:cjoasilva@ua.pt)

Departamento de Matemática da Universidade de Aveiro. Campus Universitário de Santiago, 3810-193 Aveiro, Aveiro, Portugal

Optimal control, Mathematical modelling, Applied Mathematics

Lunji Song

✉ (mailto:song@lzu.edu.cn)

School of Mathematics and Statistics, Lanzhou University, Lanzhou, 730000, China

Numerical analysis

Shiji Song



(mailto:shijis@mail.tsinghua.edu.cn)

Department of Automation, Tsinghua University, Beijing 100084, China

Control theory with applications; Mathematic Programming

Ricardo L.Soto

✉ (mailto:rsoto@ucn.cl)

Department of Mathematics, Universidad Católica del Norte, Angamos 0610. Postal Code 1270709, Antofagasta. CHILE

Nonnegative matrices, Nonnegative Inverse elementary divisors problem

Tommi Sottinen
✉ (mailto:tommi.sottinen@iki.fi)

Department of Mathematics and Statistics, University
of Vaasa, P.O. Box 700, 65101, Vaasa, Finland
*Stochastic analysis, Mathematical finance, Gaussian
processes*

Marco Squassina
✉ (mailto:marco.squassina@unicatt.it)

Dipartimento di Matematica e Fisica Università
Cattolica del Sacro Cuore Via dei Musei 41, I-25121
Brescia, Italy
Partial differential equations and Nonlinear Analysis

Martin Stoll
✉ (mailto:stollm@mpi-
magdeburg.mpg.de)

Max Planck Institute for Dynamics of Complex
Technical Systems, Sandtorstr. 139106 Magdeburg,
Germany
*Numerical Linear Algebra for Dynamical Systems,
Partial differential equations*

Chunyou Sun
✉ (mailto:sunchy@lzu.edu.cn)

School of Mathematics and Statistics, Lanzhou
University, Lanzhou, 730000, China
*Dissipative evolution PDEs in mathematical physics,
Attractors and long time dynamics*

Raafat Talhouk
✉ (mailto:rtalhouk@ul.edu.lb)

Department of Mathematics, Lebanese University,
Hadath, Lebanon
Fluid dynamics and PDEs

Kok Lay Teo
✉ (mailto:K.L.Teo@curtin.edu.au)

Department of Mathematics and Statistics, Curtin
University, GPO Box U1987, Perth Western Australia
6845, Australia
Engineering Mathematics, Optimization and Control

Shou-Fu Tian
✉ (mailto:sftian@cumt.edu.cn)

School of Mathematics, and Institute of Mathematical
Physics, China University of Mining and Technology,
Xuzhou 221116, People's Republic of China
*Nonlinear Dispersive Waves; Mathematical Physics and
Integrable Systems*

Juan R. Torregrosa
✉ (mailto:jrtorre@mat.upv.es)

Institute for Multidisciplinary Mathematics, Universitat Politècnica de València, Camino de Vera s/n, 46022 València, Spain
Iterative processes, Matrix analysis, Dynamical system

Juan Alberto Rodríguez Velázquez
✉ (mailto:juanalberto.rodriguez@urv.cat)

Universitat Rovira i Virgili, Departament d'Enginyeria Informàtica i Matemàtiques, Av. Països Catalans 26, 43007 Tarragona, Spain
Graph Theory, Combinatorics

Ezio Venturino
✉ (mailto:ezio.venturino@unito.it)

Dipartimento di Matematica, Università di Torino, via Carlo Alberto 10, 10123 Torino, Italy
Numerical analysis, Mathematical modelling

Uzi Vishne
✉ (mailto:vishne@math.biu.ac.il)

Department of Mathematics, Bar Ilan University, Ramat Gan, Israel
Ring theory, Central simple algebras, Quadratic forms

Shouhong Wang
✉ (mailto:showang@indiana.edu)

Department of mathematics, Indiana University, Bloomington, IN 47405.
Fluid and geophysical fluid dynamics, Field theory and general relativity

Yansheng Wu
✉ (mailto:yanshengwu@njupt.edu.cn)

School of Computer Science, Nanjing University of Posts and Telecommunications, Nanjing, 210023, China
Coding Theory; Discrete Mathematics; Number Theory

Chuanju Xu
✉ (mailto:cjxu@xmu.edu.cn)

School of Mathematical Sciences, Xiamen University, Xiamen, China
Numerical PDEs and Spectral methods

Shengyuan Xu
✉ (mailto:syxu02@yahoo.com.cn)

Nanjing University of Science and Technology,
Nanjing 210094, PR China
Complex systems, Delay systems, and Control theory

Ismael G. Yero
✉ (mailto:ismael.gonzalez@uca.es)

Departamento de Matemáticas, Universidad de Cádiz,
Algeciras, Spain
Graph theory, Combinatorics

Xu Zhang
✉ (mailto:zhang_xu@scu.edu.cn)

Yangtze Center of Mathematics, Sichuan University,
Chengdu 610064, China
Control theory

Shihui Zhu
✉
(mailto:shihuizhumath@sicnu.edu.cn)
✉ (mailto:shihuizhumath@163.com)

School of Mathematical Sciences, Sichuan Normal
University, Chengdu, 610066, P R China
*Nonlinear PDEs in Mathematical Physics, Blow-up and
Stability*

Mohamed Ziane
✉ (mailto:ziane@usc.edu)

University of Southern California, 3620 S. Vermont
Avenue, KAP 108, Los Angeles, CA 90089, USA
Partial Differential Equations, Navier-Stokes Equations



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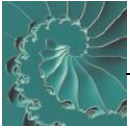
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Research article

Parameter estimation and fractional derivatives of dengue transmission model

Windarto¹, Muhammad Altaf Khan² and Fatmawati^{1,*}

¹ Department of Mathematics, Faculty of Science and Technology, Universitas Airlangga, Surabaya 60115, Indonesia

² Faculty of Natural and Agricultural Sciences, University of the Free state, South Africa

* **Correspondence:** Email: fatmawati@fst.unair.ac.id.

Abstract: In this paper, we propose a parameter estimation of dengue fever transmission model using a particle swarm optimization method. This method is applied to estimate the parameters of the host-vector and SIR type dengue transmission models by using cumulative data of dengue patient in East Java province, Indonesia. Based on the parameter values, the basic reproduction number of both models are greater than one and obtained their value for SIR is $\mathcal{R}_0 = 1.4159$ and for vector host is $\mathcal{R}_0 = 1.1474$. We then formulate the models in fractional Atangana-Baleanu derivative that possess the property of nonlocal and nonsingular kernel that has been remained effective to many real-life problems. A numerical procedure for the solution of the model SIR model is shown. Some specific numerical values are considered to obtain the graphical results for both the SIR and Vector Host model. We show that the model vector host provide good results for data fitting than that of the SIR model.

Keywords: dengue model; parameter estimation; particle swarm optimization method; Atangana-Baleanu derivative

Mathematics Subject Classification: 34A08, 92B05

1. Introduction

Dengue fever is one of the most contagious diseases in the tropics and subtropics around the world. The disease is caused by the dengue virus that is transmitted to humans through the bite of *Aedes Aegypti* female mosquito. After incubation of the virus for 4-10 days, the infected mosquito is capable of transmitting the virus for the rest of its life. The incidence of dengue globally has been widespread in recent decades. About half of the world's population is now at risk of becoming infected with this disease [1].

Compared to other diseases and their effects, dengue is a huge burden on human populations, health,

and economic systems in most tropical countries in the world. Every year, 100 out of 1000 cases increase, 20,000 of them die [2]. There is no specific treatment for dengue, but early detection and access to appropriate medical care reduce mortality. Prevention and control of dengue depend on effective vector control [1].

In Indonesia, dengue fever is one of the infectious diseases that until now is still a public health problem. This disease often appears as an extraordinary event because of its rapid and potentially deadly spread. Dengue fever spread throughout Indonesia and attacked all age groups, especially children since it was first discovered in 1968 in Surabaya [3]. In 2013, the number of dengue fever patients in Indonesia reported as many as 112,511 cases with the death of 871 people [4].

The mathematical modeling has become a powerful tool for understanding the dynamics of the spread of an infectious disease including dengue fever. Some researchers have developed a mathematical model of the spread of dengue fever with a host and vector approach [5–7]. A mathematical model cannot be interpreted in real cases if the parameter values of the model are unknown. Pandey et al. in [8] have applied Bayesian Markov chain Monte Carlo (MCMC) method to estimate the parameters of simple host-vector and SIR (Susceptible, Infectious, Recovery) model using monthly incidence of dengue fever in Thailand. The comparison result show that the SIR model better than the host-vector model to explain the incidence data from Thailand. Gotz et al. [9] linked daily data of dengue and rainfall patients in Semarang city, Indonesia to estimate IR (Infectious, Recovery) model with optimal control theory approach. Recently, Agosto and Khan [10] have parameterized the dengue model using the classical least-squares method based on the 2017 dengue data in Pakistan.

When a mathematical model was presented in a closed form, then the parameters in the model can be estimated by deterministic optimization methods such as the Newton method or Nelder-Mead method [11]. Unfortunately, the Nelder-Mead or Newton method fails to converge into global minimum of a function if the function has many local minima [12]. In addition, many mathematical models occur in non-linear ODE (ordinary differential equation) systems, so the exact solution (closed form solution) of the model cannot be obtained. In this case, a heuristic method can be used to estimate parameter values from a non-linear model or a non-linear ODE system. Heuristic method such as Genetic Algorithm (GA) and Particle Swarm Optimization (PSO) method have been previously used to estimate parameters of non-linear ordinary differential equations system model. GA method has been often employed to optimize the parameters of ODE model [13–15]. So far the PSO method is rarely explored in this field [16, 17]. PSO method was developed by Kennedy and Eberhart in 1995 [18]. This method is inspired by social behavior of organisms in a group e.g. bird swarm, fish swarm and ant colony.

In the present era the fractional order models associated with epidemic models gaining much attention day by day. The development in fractional calculus in terms of fractional derivative and the relevant definitions are proposed, Caputo, Caputo-Fabrizio and Atangana-Baleanu derivative. These derivative have successfully applied to the models of real-life problems and obtained good results [19–25]. The Atangana-Baleanu is the recent development in the fractional calculus and getting attention day by day due to its memory effect [26]. This derivative is based on nonlocal and non-singular kernel and can handle the problems associated to real life situations. The crossover behavior and the non-local dynamics of the realistic models cannot be utilized efficiently with the integer derivative and to such problems the role of fractional calculus is appreciated. More recently,

Qureshi and Atangana [27] have compared the integer and fractional derivative dengue models related to dengue fever outbreak in Cape Verde islands around 2009.

In this paper, we propose the parameter estimation techniques with PSO method. This method is applied to estimate the parameters of the host-vector and SIR type dengue fever transmission model based on cumulative data of dengue fever patient in East Java province, Indonesia. Furthermore, we formulate the dengue transmission model of the host-vector and SIR type in Atangana-Baleanu derivative. The numerical procedure for Atangana-Baleanu derivative is then implemented for different values of the fractional order of the model.

2. Host-vector model for dengue transmission

In this section, we describe a simple host-vector model for dengue transmission. Here we follow the host-vector model from [8, 19] to describe the dynamics of dengue disease transmission. We also apply the model to explain dengue transmission in East Java province, Indonesia. We included the disease-induced mortality in human population (host). The host-vector model is divided into three human host populations, susceptible (S), infectious (I) and recovered (R), and two mosquitoes (vector) populations, susceptible (V_S) and infectious (V_I). The system of differential equations describing the host-vector model is written as

$$\begin{aligned}
 \frac{dS}{dt} &= \Lambda - \beta_h \frac{V_I}{V} S - \mu S, \\
 \frac{dI}{dt} &= \beta_h \frac{V_I}{V} S - (\gamma + \mu + d)I, \\
 \frac{dR}{dt} &= \gamma I - \mu R, \\
 \frac{dV_S}{dt} &= \Lambda_v - \beta_v \frac{I}{N} V_S - \mu_v V_S, \\
 \frac{dV_I}{dt} &= \beta_v \frac{I}{N} V_S - \mu_v V_I,
 \end{aligned} \tag{2.1}$$

where $N = S + I + R$ and $V = V_S + V_I$ denote the total population size of host and vector, respectively. Parameter description of model (2.1) could be seen in Table 1.

Table 1. Parameters of model (2.1).

| Description | Parameter |
|---|-------------|
| Recruitment rate of host | Λ |
| Recruitment rate of vector | Λ_v |
| Natural death rate of host | μ |
| Natural death rate of vector | μ_v |
| The vector-to-host transmission probability | β_h |
| The host-to-vector transmission probability | β_v |
| Recovery rate | γ |
| Disease induced death rate for host | d |

The change rate of the total human populations is given by

$$\frac{dN}{dt} = \Lambda - \mu N - dI,$$

and the change rate of the total vector populations is as follow

$$\frac{dV}{dt} = \Lambda_v - \mu_v V.$$

It is noted that in the absence of the disease-induced death ($d = 0$), the total human population, $N \rightarrow \frac{\Lambda}{\mu}$ as $t \rightarrow \infty$. The biologically feasible region of the model (2.1) consisting of

$$\Omega_h \times \Omega_v \subset \mathbb{R}_+^3 \times \mathbb{R}_+^2,$$

with

$$\Omega_h = \left\{ (S, I, R) \in \mathbb{R}_+^3 : 0 \leq N \leq \frac{\Lambda}{\mu} \right\},$$

and

$$\Omega_v = \left\{ (V_S, V_I) \in \mathbb{R}_+^2 : 0 \leq V \leq \frac{\Lambda_v}{\mu_v} \right\}.$$

As the standard analysis of the model, we begin by calculating the basic reproduction number of the model. The basic reproduction number is the expected number of secondary case per primary case in a virgin population [28, 29]. The model (2.1) has two equilibriums, namely the disease-free equilibrium and the endemic equilibrium. The disease-free equilibrium of model (2.1) is given by $E^0 = (S^0, I^0, R^0, V_S^0, V_I^0) = (\frac{\Lambda}{\mu}, 0, 0, \frac{\Lambda_v}{\mu_v}, 0)$. Using the next generation method [30], the basic reproduction number of the model (2.1) is

$$\mathcal{R}_0 = \sqrt{\frac{\beta_h \beta_v}{\mu_v (\gamma + \mu + d)}}. \quad (2.2)$$

The disease-free equilibrium of model (2.1) is locally asymptotically stable if $\mathcal{R}_0 < 1$, however the endemic equilibrium locally asymptotically stable if $\mathcal{R}_0 > 1$.

In order to parameterize dengue model (2.1), we assumed that the total human population (N) is a constant due to we only fit the data to the model about one year. We also assumed that the total vector populations is the constant. Thus, we choose $\Lambda = \mu N + dI$ and $\Lambda_v = \mu_v V$. Hence, the mathematical model (2.1) can be written follow

$$\begin{aligned} \frac{dN}{dt} &= 0, \\ \frac{dI}{dt} &= \beta_h \frac{V_I}{V} (N - I - R) - (\gamma + \mu + d)I, \\ \frac{dR}{dt} &= \gamma I - \mu R, \end{aligned} \quad (2.3)$$

$$\begin{aligned}\frac{dV}{dt} &= 0, \\ \frac{dV_I}{dt} &= \beta_v \frac{I}{N}(V - V_I) - \mu_v V_I.\end{aligned}$$

There are six unknown parameters in host-vector model (2.3) i.e. $\beta_h, \mu, \gamma, d, \beta_v$ and μ_v . The six parameters of the model (2.3) were estimated using dengue fever data obtained from East Java province using particle swarm optimization method.

3. SIR model for dengue transmission

Most of the mathematical models for dengue fever transmission have been developed with the host-vector model approach. However, vector population (mosquito) data in the field is usually difficult to obtain because of the infection dynamics in the vectors are faster than in the hosts (humans). In terms of estimating the model parameters, it is more appropriate to model the spread of dengue using the SIR-type. The dengue transmission model using SIR-type is represented by the following equations

$$\begin{aligned}\frac{dS}{dt} &= \Lambda - \beta \frac{I}{N}S - \mu S, \\ \frac{dI}{dt} &= \beta \frac{I}{N}S - (\gamma + \mu + d)I, \\ \frac{dR}{dt} &= \gamma I - \mu R,\end{aligned}\tag{3.1}$$

where S, I and R denote the susceptible, infected and recovered human populations respectively. The parameters Λ denote the birth rate, β denote the rate for dengue transmission and μ denote natural death rate. By γ we denote the recovery rate and d denote dengue death rate. All parameters of the model (3.1) are assumed to be constant and nonnegative. If we assume N denotes the total human population, then we have $N = S + I + R$. The change rate of the total populations is given by

$$\frac{dN}{dt} = \Lambda - \mu N - dI.\tag{3.2}$$

The model (3.1) has the biologically feasible region on Ω with

$$\Omega = \left\{ (S, I, R) \in \mathbb{R}_+^3 : 0 \leq N \leq \frac{\Lambda}{\mu} \right\}.$$

The model (3.1) has a disease free equilibrium $E_0 = (S_0, I_0, R_0) = (\frac{\Lambda}{\mu}, 0, 0)$. Using the next generation method as presented in [30], the basic reproduction number of the model (3.1) is

$$\mathcal{R}_0 = \frac{\beta}{\gamma + \mu + d}.\tag{3.3}$$

Thus, the endemic equilibrium of the model (3.1) is given by $E^* = \left(\frac{(\gamma + \mu + d)\Lambda}{\mu\beta}, \frac{\Lambda}{\beta}(\mathcal{R}_0 - 1), \frac{\gamma\Lambda}{\mu\beta}(\mathcal{R}_0 - 1) \right)$. The disease-free equilibrium of model (3.1) is locally asymptotically stable if $\mathcal{R}_0 < 1$. Meanwhile, the endemic equilibrium is exists and locally asymptotically stable if $\mathcal{R}_0 > 1$.

Next, for the simplicity we assumed the total population (N) was constant by using $\Lambda = \mu N + dI$. Thus, the mathematical model (3.1) can be expressed as follows.

$$\begin{aligned}\frac{dN}{dt} &= 0 \\ \frac{dI}{dt} &= \beta \frac{I}{N}(N - I - R) - (\gamma + \mu + d)I, \\ \frac{dR}{dt} &= \gamma I - \mu R.\end{aligned}\tag{3.4}$$

In the next section, we estimate all parameters in the model (3.4). The model has four parameters i.e. β, μ, γ , and d . We apply the genetic algorithm to estimate all parameters in the model.

4. Parameter estimation using particle swarm optimization method

In this method, solutions are represented by particles. A particle is represented by the position of the particle (x_i) and the particle velocity (v_i). This method begins with random selection of particle position and particle velocity.

Motion of a particle is influenced by stochastic and deterministic components. Every particle is influenced by global-best position (g_{best}) and particle-best position in a particle group (p_{best}). In general, the parameter estimation step by using the particle swarm optimization method is as follows:

- (a) Evaluate cost function value of every particle. Here we choose mean absolute percentage error (MAPE) as a cost function which is given by

$$x = \frac{\sum_{i=1}^n \left(\frac{\sum_{j=1}^3 \frac{|y_{ij} - y_{ij}^*|}{y_{ij}}}{3} \right)}{n}.\tag{4.1}$$

Here n is the number of data, y_{ij} is the real data component, and y_{ij}^* is the component of the solution of the differential equation using the Runge-Kutta method.

- (b) Update the particle best (p_{best}) and the global best (g_{best}). Let the particle swarm optimization method contains m particles. At every iteration, the particle-best position ($p_{(best,i)}(t)$) is replaced by position of current particle $x_i(t + 1)$ when the MAPE of $x_i(t + 1)$ is lower than the MAPE of $p_{(best,i)}(t)$. Moreover, and the global best position (g_{best}) is substituted by position of the current particle $x_i(t + 1)$ when the MAPE of $x_i(t + 1)$ is lower than the MAPE of $g_{best}(t)$.
- (c) Calculate new velocity of every particle by using

$$v_i(t + 1) = wv_i(t) + c_1r_1(p_{best}(t) - x_i(t)) + c_2r_2(g_{best}(t) - x_i(t));\tag{4.2}$$

Here r_1 and r_2 are random numbers between zero and one with uniform distribution.

- (d) Calculate new position of every particle by using

$$x_i(t + 1) = x_i(t) + v_i(t + 1)\tag{4.3}$$

The steps are reiterated some termination condition is met. Here we choose $c_1 = c_2 = 2$ and $w = 1$.

5. Parameter estimation of host-vector and SIR model

East Java Province is located in the eastern part of the island of Java, Indonesia. The population is about $N = 41.5$ millions [31]. East Java has the widest area among 6 provinces in Java Island and has the second largest population in Indonesia after West Java. The data used for parameter estimation on the SIR-type model is cumulative data of dengue fever case per month from March 2012 - February 2013 presented in Figure 1 [3]. The data represent data of dengue epidemic condition in East Java. Cumulative data are generally smoother than actual event data and it is also easier to handle data delays due to holidays and weekends [8].

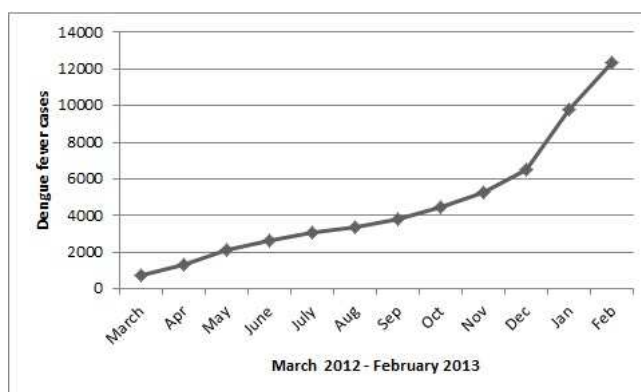


Figure 1. Cumulative dengue fever incidence in East-Java Indonesia from March 2012 to February 2013.

In this section, we estimate parameters of host-vector model (2.3) and SIR model (3.4) by using PSO method. We estimated parameters in the host-vector and SIR such that the mean absolute percentage error (MAPE) is minimum. In the PSO implementation, the number of particles is set to 40 particles. We applied the methods for 20 trials where for every trial the methods were terminated after 250 iterations. The best results of the host-vector model and SIR model are presented in the Table 2 and Table 3 respectively.

Table 2. The best estimation results of the host-vector model.

| β_h | β_v | μ | γ | μ_v | d | MAPE |
|-----------|-----------|----------|----------|----------|----------|----------|
| 1.361353 | 1.255105 | 0.001185 | 0.224115 | 1.415122 | 0.691767 | 0.077705 |

Table 3. The best estimation results of the SIR model.

| β | μ | γ | d | MAPE |
|----------|----------|----------|----------|----------|
| 0.888349 | 0.001185 | 0.262486 | 0.363749 | 0.116089 |

From the Tables 2 and 3, minimum of MAPE of the host-vector and SIR model are around 7.77 % and 11.61 % respectively. By using parameter values from the tables, we find the basic reproduction number for the host-vector model and the SIR model are

$$R_{0,Host-Vector} = 1.147434, R_{0,SIR} = 1.415876. \quad (5.1)$$

respectively. The basic reproduction number values from both models indicates dengue endemic condition in East Java province, Indonesia. This prediction result is consistent with the real situation, where dengue infection is not removed yet from the East Java province.

Figures 2 and 3 illustrate both models matching images with real data. From Figure 2 it can be seen that the number of infected humans of the SIR model between estimation results with real data is very close at the end of the observation although there is a small deviation at the beginning. However, the estimated result of the host-vector model for the infected human is very closed for the first 10 months and then there is a small deviation at the end of the observation. Similarly, in Figure 3 indicates that the number of recovered human of both models between estimation results and real data is also quite close until the end of the observation. Hence, we will explore the two dengue models with a fractional model approach in order to see the comparison with real data.

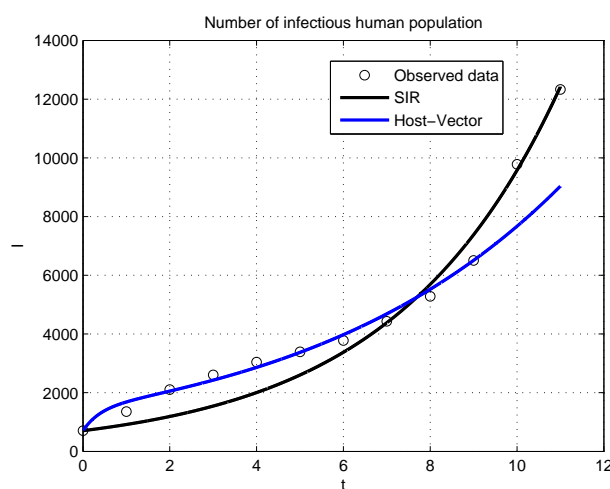


Figure 2. The estimates of human infections to the data.

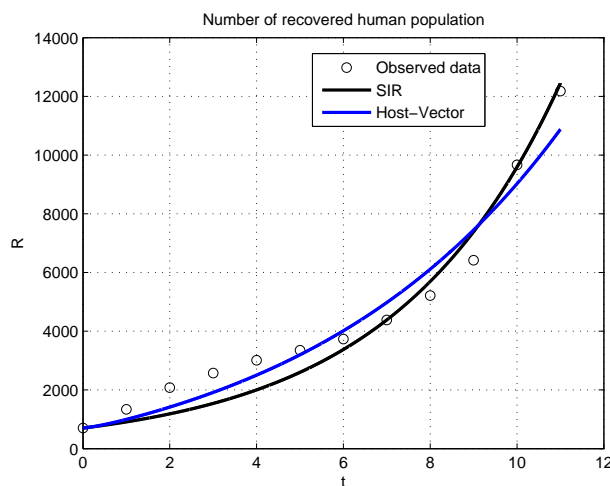


Figure 3. The estimates of human recovery to the data.

6. A fractional dengue model

The present section presents the dengue SIR model given in (3.1), will be formulated in Atangana-Baleanu derivative. Therefore, the fractional Atangana-Baleanu representation for the SIR dengue model (3.1) take the shape below:

$$\begin{cases} {}_0^{AB}D_t^\alpha S = \Lambda - \beta \frac{I}{N}S - \mu S, \\ {}_0^{AB}D_t^\alpha I = \beta \frac{I}{N}S - (\gamma + \mu + d)I, \\ {}_0^{AB}D_t^\alpha R = \gamma I - \mu R, \end{cases} \quad (6.1)$$

where, S , I and R and their parameters defined in above sections. Further, the initial conditions associated with the model (6.1) are non-negative. Before working on the model (6.1), first, we present the basic definitions related to the fractional Atangana-Baleanu derivative and then, we give the numerical procedure to obtain the graphical results of the model with various fractional values of the fractional order parameter α . The Vector host model in the form of Atangana-Baleanu derivative can be expressed as

$$\begin{cases} {}_0^{AB}D_t^\alpha S = \Lambda - \beta_h \frac{V_I}{V}S - \mu S, \\ {}_0^{AB}D_t^\alpha I = \beta_h \frac{V_I}{V}S - (\gamma + \mu + d)I, \\ {}_0^{AB}D_t^\alpha R = \gamma I - \mu R, \\ {}_0^{AB}D_t^\alpha V_S = \Lambda_v - \beta_v \frac{I}{N}V_S - \mu_v V_S, \\ {}_0^{AB}D_t^\alpha V_I = \beta_v \frac{I}{N}V_S - \mu_v V_I. \end{cases} \quad (6.2)$$

In the numerical section, we give a numerical procedure for the solution of the SIR model in Atangana-Balenau derivative (6.1) and for the vector host model in fractional derivative (6.2) the readers can easily implement a numerical scheme by following the procedure given for (6.1).

6.1. Basic concepts of A-B derivative

First, we give some definitions on A-B fractional derivative which will be used later in our study [26].

Definition 6.1. Suppose $h \in F^1(a, b)$, $b > a$, $\alpha \in [0, 1]$ then in Caputo sense the newly fractional derivative can be written as follows:

$${}_a^{AB}D_t^\alpha(h(t)) = \frac{B(\alpha)}{1-\alpha} \int_a^t h'(\chi) E_\alpha \left[-\alpha \frac{(t-\chi)^\alpha}{1-\alpha} \right] d\chi,$$

where $B(\alpha) = 1 - \alpha + \frac{\alpha}{\Gamma(\alpha)}$ is a normalized function with $B(0) = B(1) = 1$ and E_α is Mittag-Leffler function

$$E_\alpha(z) = \sum_{k=0}^{\infty} \frac{(z)^k}{\Gamma(\alpha k + 1)}, \alpha > 0.$$

Definition 6.2. Consider $h \in F^1(a, b)$, $b > a$, $\alpha \in [0, 1]$, (not necessary differentiable) then, in Riemann-Liouville (ABR) sense, one can express the newly derivative knows as Atangana-Baleanu fractional derivative as is follows:

$${}_a^{ABR}D_t^\alpha(h(t)) = \frac{B(\alpha)}{1-\alpha} \frac{d}{dt} \int_a^t h(\chi) E_\alpha \left[-\alpha \frac{(t-\chi)^\alpha}{1-\alpha} \right] d\chi.$$

Definition 6.3. For the Atangana-Baleanu fractional derivative one can express the fractional integral with non local kernel as follows:

$${}_{a}^{AB}I_t^\alpha(h(t)) = \frac{1-\alpha}{B(\alpha)}h(t) + \frac{\alpha}{B(\alpha)\Gamma(\alpha)} \int_a^t h(y)(t-y)^{\alpha-1}dy.$$

We obtain the initial function and the classical integral respectively, when the fractional order is zero and 1.

Theorem 6.4. On $[a, b]$, the following inequality holds for f when the function h is continuous on $[a, b]$.

$$\|{}_{a}^{ABR}D_t^\alpha(h(t))\| < \frac{B(\alpha)}{1-\alpha} \|h(x)\|, \text{ where } \|h(x)\| = \max_{a \leq x \leq b} |h(x)|. \quad (6.3)$$

Theorem 6.5. Atangana-Baleanu and Atanagan-Baleanu-R derivatives both fulfill the condition Lipschitz given in the following:

$$\|{}_{a}^{AB}D_t^\alpha h_1(t) - {}_{a}^{ABC}D_t^\alpha h_2(t)\| < K \|h_1(t) - h_2(t)\|, \quad (6.4)$$

also for ABR derivative we have

$$\|{}_{a}^{ABR}D_t^\alpha h_1(t) - {}_{a}^{ABR}D_t^\alpha h_2(t)\| < K \|h_1(t) - h_2(t)\|. \quad (6.5)$$

Theorem 6.6. For the FDE

$${}_{a}^{AB}D_t^\alpha h(t) = s(t), \quad (6.6)$$

one can obtain a unique solution by using the inverse Laplace transform and the convolution result [26]:

$$h(t) = \frac{1-\alpha}{AB(\alpha)}s(t) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \int_a^t s(\xi)(t-\xi)^{\alpha-1}d\xi. \quad (6.7)$$

7. Numerical procedure

The aim of the present section is to obtain the numerical results of the model (6.1) using the method in [32] which is applied efficiently to various kind of real-life problems such as [21–23]. Now using this technique we apply to our model (6.1) as follows:

For the simplification purpose, we express the model (6.1) in the following form:

$$\begin{aligned} {}_0^{AB}D_t^\alpha S &= \mathcal{K}_1(t, S, I, R), \\ {}_0^{AB}D_t^\alpha I &= \mathcal{K}_2(t, S, I, R), \\ {}_0^{AB}D_t^\alpha R &= \mathcal{K}_3(t, S, I, R). \end{aligned} \quad (7.1)$$

System (6.1) can be converted in the following form using the fundamental theorem of integration.

$$\begin{aligned} S(t) - S(0) &= \frac{(1-\alpha)}{AB(\alpha)}\mathcal{K}_1(t, S) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \int_0^t \mathcal{K}_1(\xi, S)(t-\xi)^{\alpha-1}d\xi, \\ I(t) - I(0) &= \frac{(1-\alpha)}{AB(\alpha)}\mathcal{K}_2(t, I) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \int_0^t \mathcal{K}_2(\xi, I)(t-\xi)^{\alpha-1}d\xi, \\ R(t) - R(0) &= \frac{(1-\alpha)}{AB(\alpha)}\mathcal{K}_3(t, R) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \int_0^t \mathcal{K}_3(\xi, R)(t-\xi)^{\alpha-1}d\xi. \end{aligned} \quad (7.2)$$

For $t = t_{n+1}$, $n = 0, 1, 2, \dots$, we obtain from Eq (7.2)

$$\begin{aligned} S(t_{n+1}) - S(t_0) &= \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_1(t_n, S) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \sum_{k=0}^n \int_{t_k}^{t_{k+1}} \mathcal{K}_1(\tau, S)(t_{n+1} - \tau)^{\alpha-1} d\tau, \\ I(t_{n+1}) - I(t_0) &= \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_2(t_n, I) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \sum_{k=0}^n \int_{t_k}^{t_{k+1}} \mathcal{K}_2(\tau, I)(t_{n+1} - \tau)^{\alpha-1} d\tau, \\ R(t_{n+1}) - R(t_0) &= \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_3(t_n, R) + \frac{\alpha}{AB(\alpha)\Gamma(\alpha)} \sum_{k=0}^n \int_{t_k}^{t_{k+1}} \mathcal{K}_3(\tau, R)(t_{n+1} - \tau)^{\alpha-1} d\tau, \end{aligned} \quad (7.3)$$

Approximating the integral in Eq (7.3), using two-point interpolation polynomial and then simplifying, we finally get the following iterative solution for the model given (6.1). In a similar way for the rest of equations of the system (6.1), we obtained the recursive formula as below

$$\begin{aligned} S(t_{n+1}) &= S(t_0) + \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_1(t_n, S) + \frac{\alpha}{AB(\alpha)} \times \\ &\quad \sum_{k=0}^n \left(\frac{h^\alpha \mathcal{K}_1(t_k, S)}{\Gamma(\alpha+2)} ((n+1-k)^\alpha (n-k+2+\alpha) - (n-k)^\alpha (n-k+2+2\alpha)) \right. \\ &\quad \left. - \frac{h^\alpha \mathcal{K}_1(t_{k-1}, S)}{\Gamma(\alpha+2)} ((n+1-k)^{\alpha+1} - (n-k)^\alpha (n-k+1+\alpha)) \right), \end{aligned} \quad (7.4)$$

$$\begin{aligned} I(t_{n+1}) &= I(t_0) + \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_2(t_n, I) + \frac{\alpha}{AB(\alpha)} \times \\ &\quad \sum_{k=0}^n \left(\frac{h^\alpha \mathcal{K}_2(t_k, I)}{\Gamma(\alpha+2)} ((n+1-k)^\alpha (n-k+2+\alpha) - (n-k)^\alpha (n-k+2+2\alpha)) \right. \\ &\quad \left. - \frac{h^\alpha \mathcal{K}_2(t_{k-1}, I)}{\Gamma(\alpha+2)} ((n+1-k)^{\alpha+1} - (n-k)^\alpha (n-k+1+\alpha)) \right), \end{aligned} \quad (7.5)$$

$$\begin{aligned} R(t_{n+1}) &= R(t_0) + \frac{1-\alpha}{AB(\alpha)} \mathcal{K}_3(t_n, R) + \frac{\alpha}{AB(\alpha)} \times \\ &\quad \sum_{k=0}^n \left(\frac{h^\alpha \mathcal{K}_3(t_k, R)}{\Gamma(\alpha+2)} ((n+1-k)^\alpha (n-k+2+\alpha) - (n-k)^\alpha (n-k+2+2\alpha)) \right. \\ &\quad \left. - \frac{h^\alpha \mathcal{K}_3(t_{k-1}, R)}{\Gamma(\alpha+2)} ((n+1-k)^{\alpha+1} - (n-k)^\alpha (n-k+1+\alpha)) \right). \end{aligned} \quad (7.6)$$

After the successful implementation of the numerical scheme on the fractional model (6.1) as explained above, we find the graphical results of the model (6.1), by considering and assigning values to the fractional parameter $\alpha \in [0, 1]$, and to the model relevant parameters.

The parameters used in numerical simulations are estimated from the real data given in Table 2 for the host-vector model and in Table 3 for the SIR model. The value of recruitment rate of host and vector are $\Lambda = 41,539.567095$ and $\Lambda_v = 787,736.152032$ respectively. The initial values of the host-vector model (2.1) and SIR model (3.1) are given by

$(S(0), I(0), R(0), V_S(0), V_I(0)) = (35054487; 706; 700; 556656; 33)$ and $(S(0), I(0), R(0)) = (35054487; 706; 700)$ respectively. We obtained Figure 4 with subgraphs (a) and (b) by using the real data and its comparison with the fractional order parameter α . We make a little change in the parameter value of $\beta_h = 1.361353$ by $\beta_h = 1.461353$ and then checked for different value of α and observed that fractional order provide good fitting to the real data. The graphical results for fractional SIR model (6.1) and vector host model (6.2) are shown respectively in Figures 5–8 and 9–12.

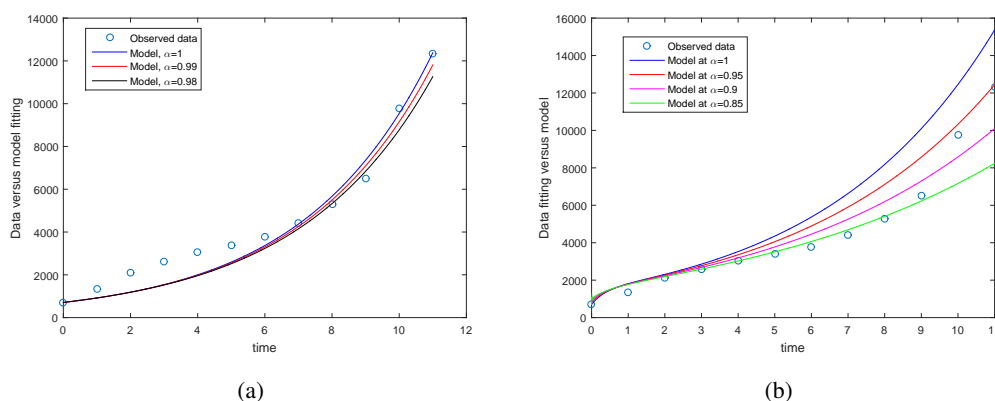


Figure 4. Numerical results for SIR fractional model (6.1) when $\alpha = 1, 0.99, 0.98$ versus data fitting Figure 4(a) and Numerical results for Vector host fractional model (6.1) when $\alpha = 1, 0.95, 0.90, 0.85$ versus data fitting Figure 4(b) .

8. Conclusion

In this study, the particle swarm optimization is implemented to estimate the parameters of the dengue transmission model using host-vector and SIR-type. The parameters of both models are estimated using the cumulative data of dengue fever patient in East Java province, Indonesia. The mean absolute percentage error of the host-vector and SIR model are around 7.77 % and 11.61 % respectively. From the parameter values, the basic reproduction number of both models are greater than one. This prediction result is consistent with the real situation, where dengue infection has not removed yet from the East Java province. Further, we formulated the host-vector and SIR models in Atangana-Baleanu fractional derivative due to the reason of non-singular and non-local kernel which effectively handled the problems of real life phenomenon which is not handled by the ordinary order derivative. Therefore, to use the advantage of the Atangana-Baleanu fractional order derivative, the results are obtained and discussed with the newly proposed procedure which is applied effectively to many real life problems. The graphical results obtained for both the fractional dengue model (6.1) and (6.2) and considered the value of $\alpha = 1, 0.95, 0.9, 0.85$. The graphical results show that at each instant of time level as well as at arbitrary derivative, one can obtain resealable information which is not possible in the case of integer order derivative. We proven that the vector host model provide better result for the dengue data rather than SIR model.

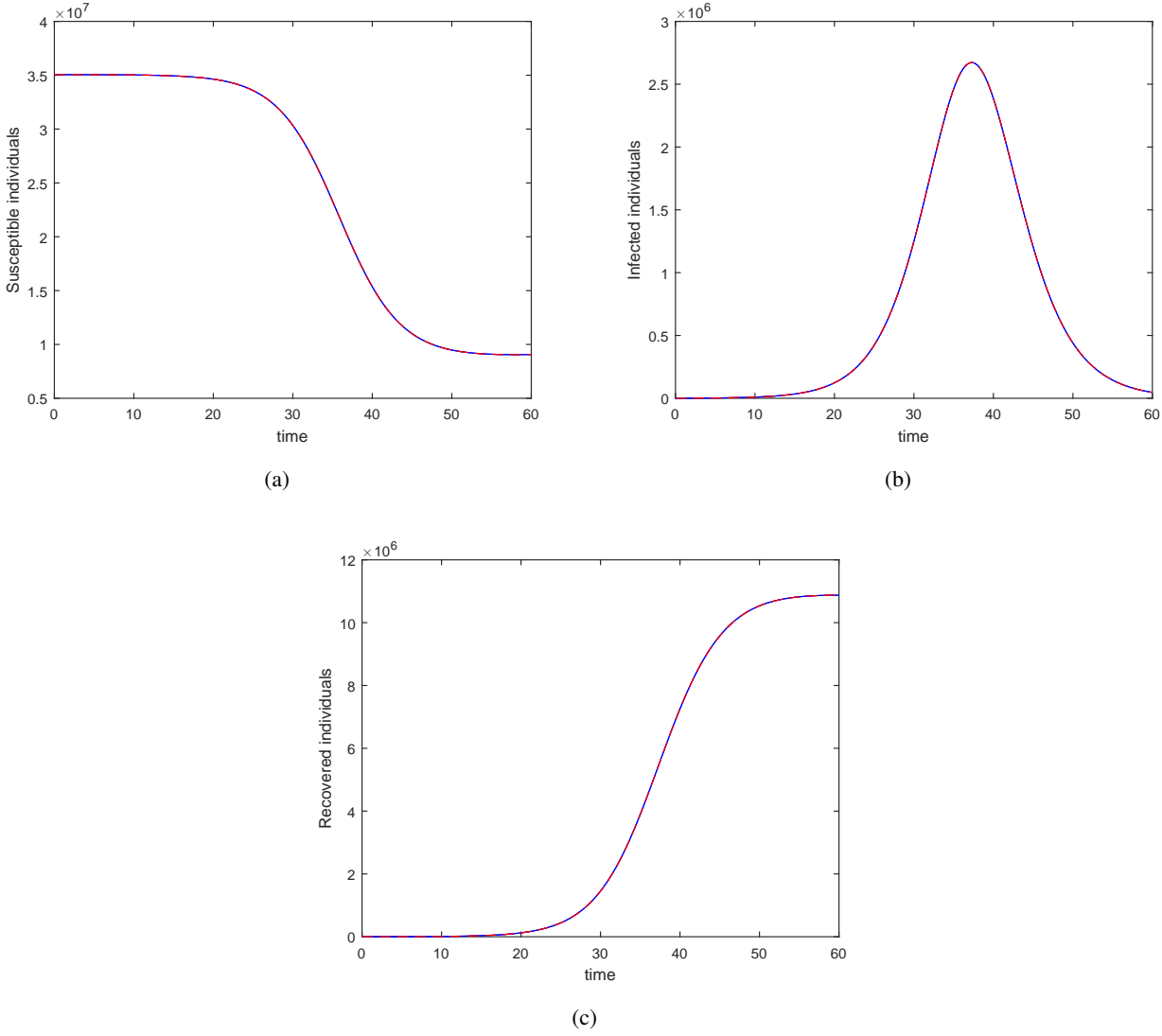


Figure 5. Numerical result for SIR model when $\alpha = 1$.

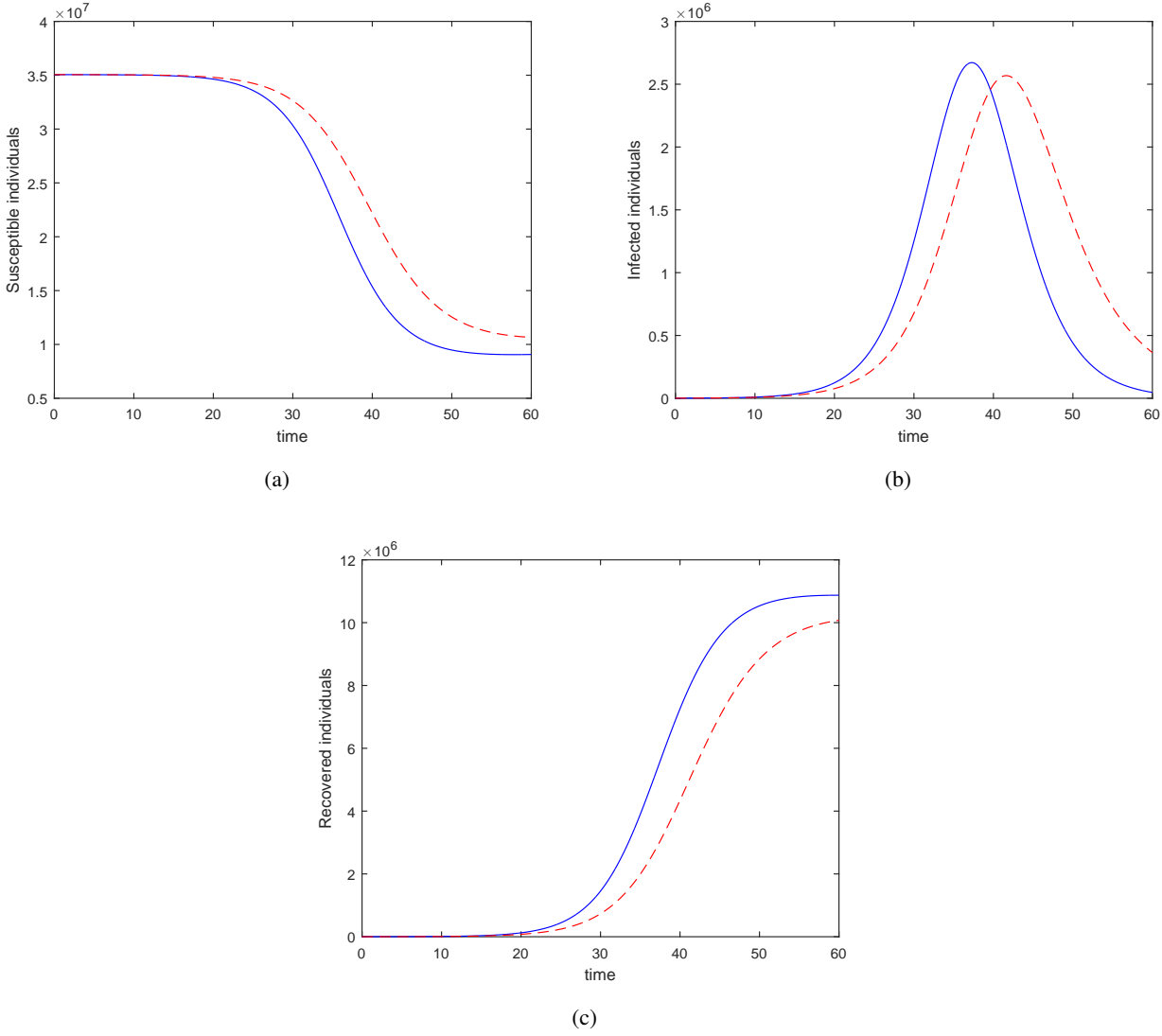


Figure 6. Numerical result for SIR model when $\alpha = 0.95$.

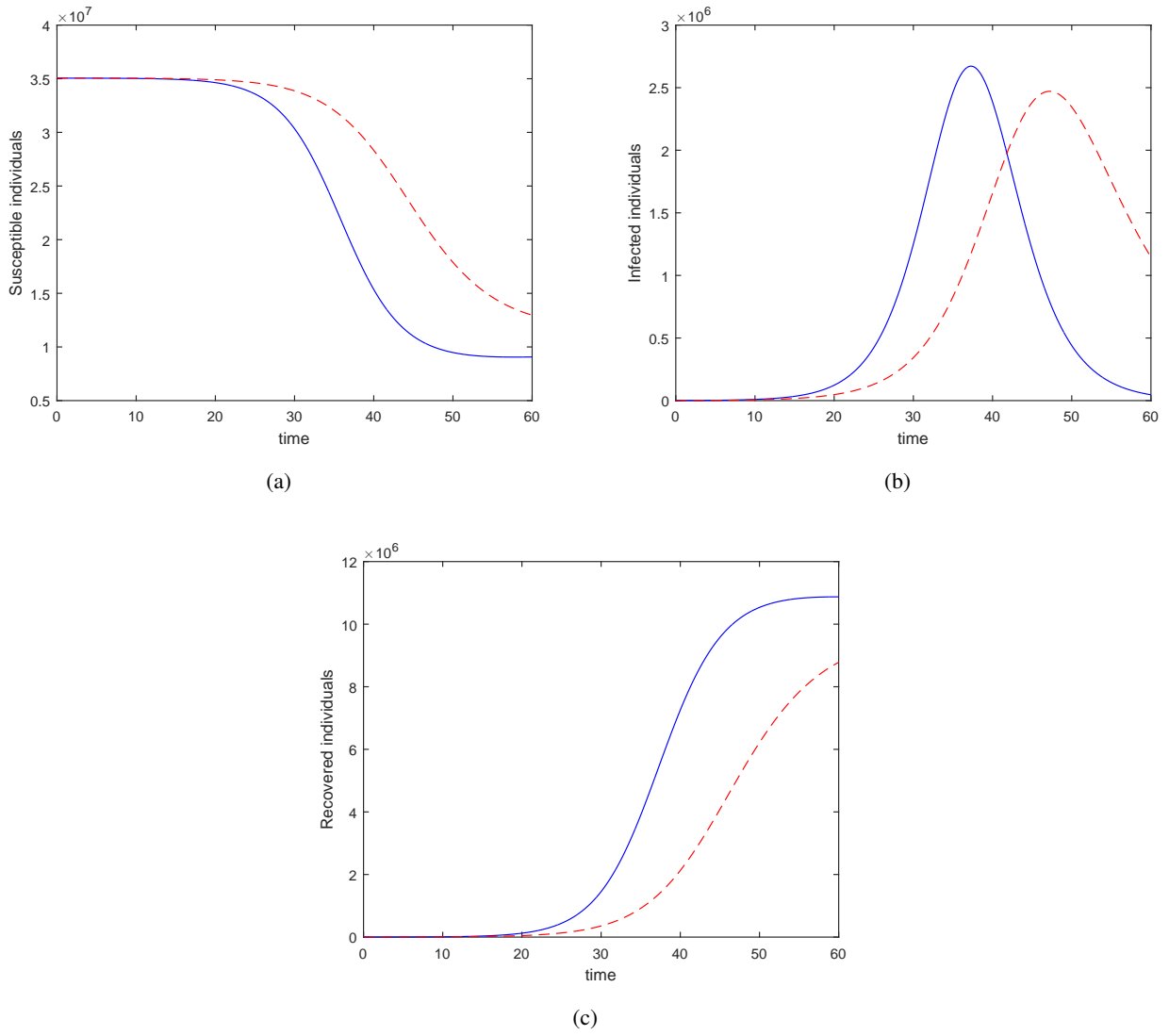


Figure 7. Numerical result for SIR model when $\alpha = 0.9$.

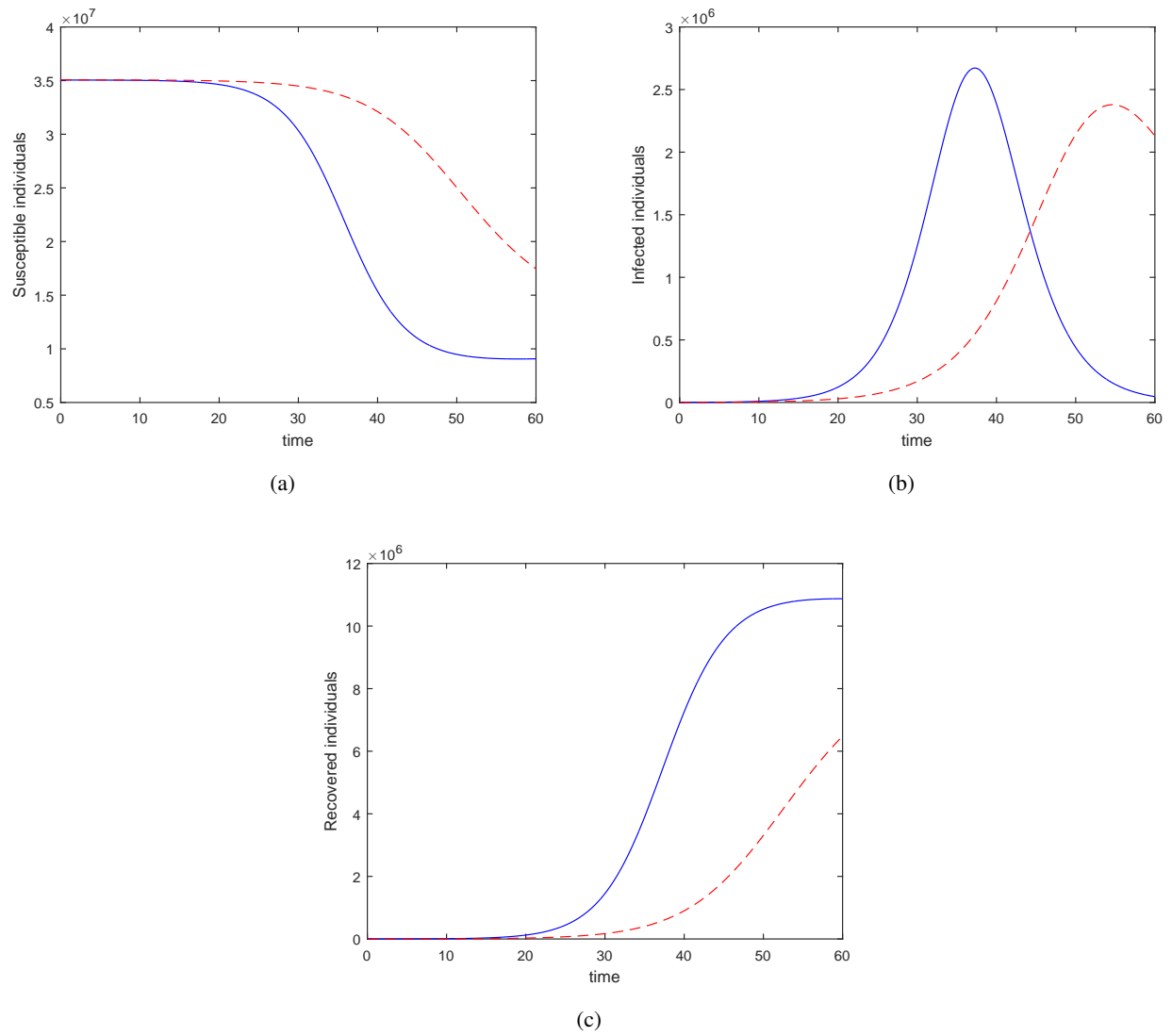


Figure 8. Numerical result for SIR model when $\alpha = 0.85$.

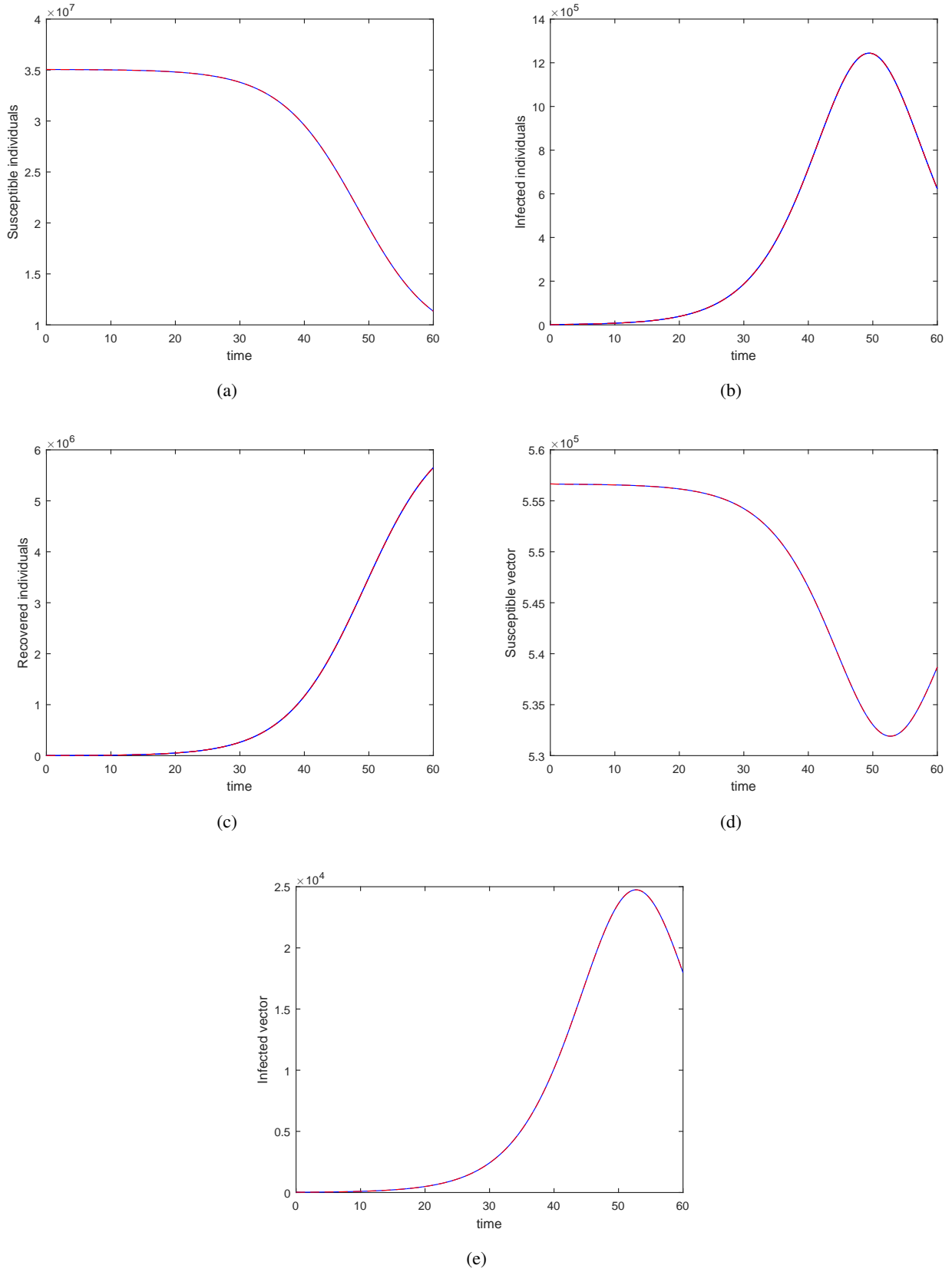


Figure 9. Numerical result for Vector host model (6.2) when $\alpha = 1$.

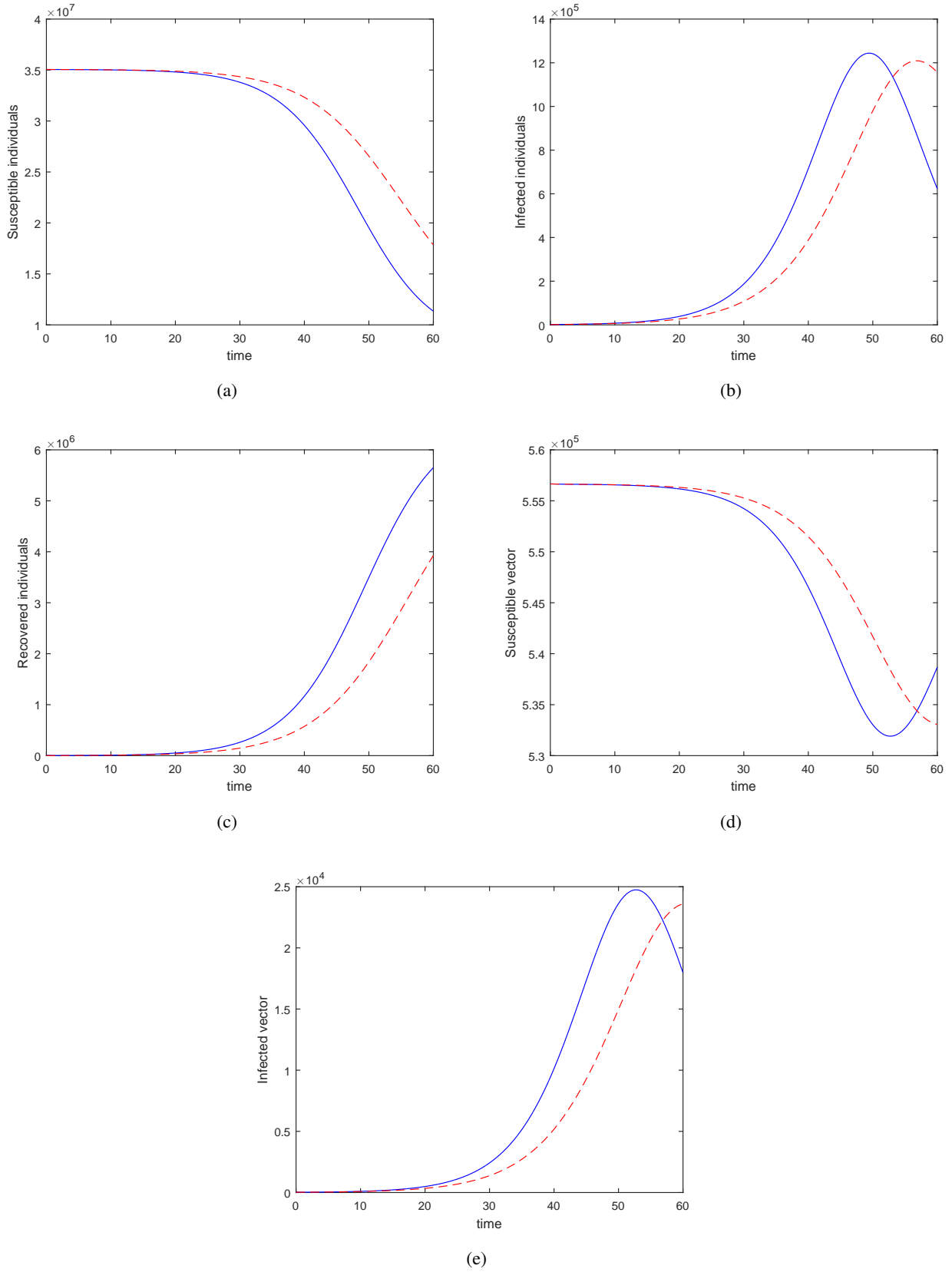


Figure 10. Numerical result for Vector host model (6.2) when $\alpha = 0.95$.

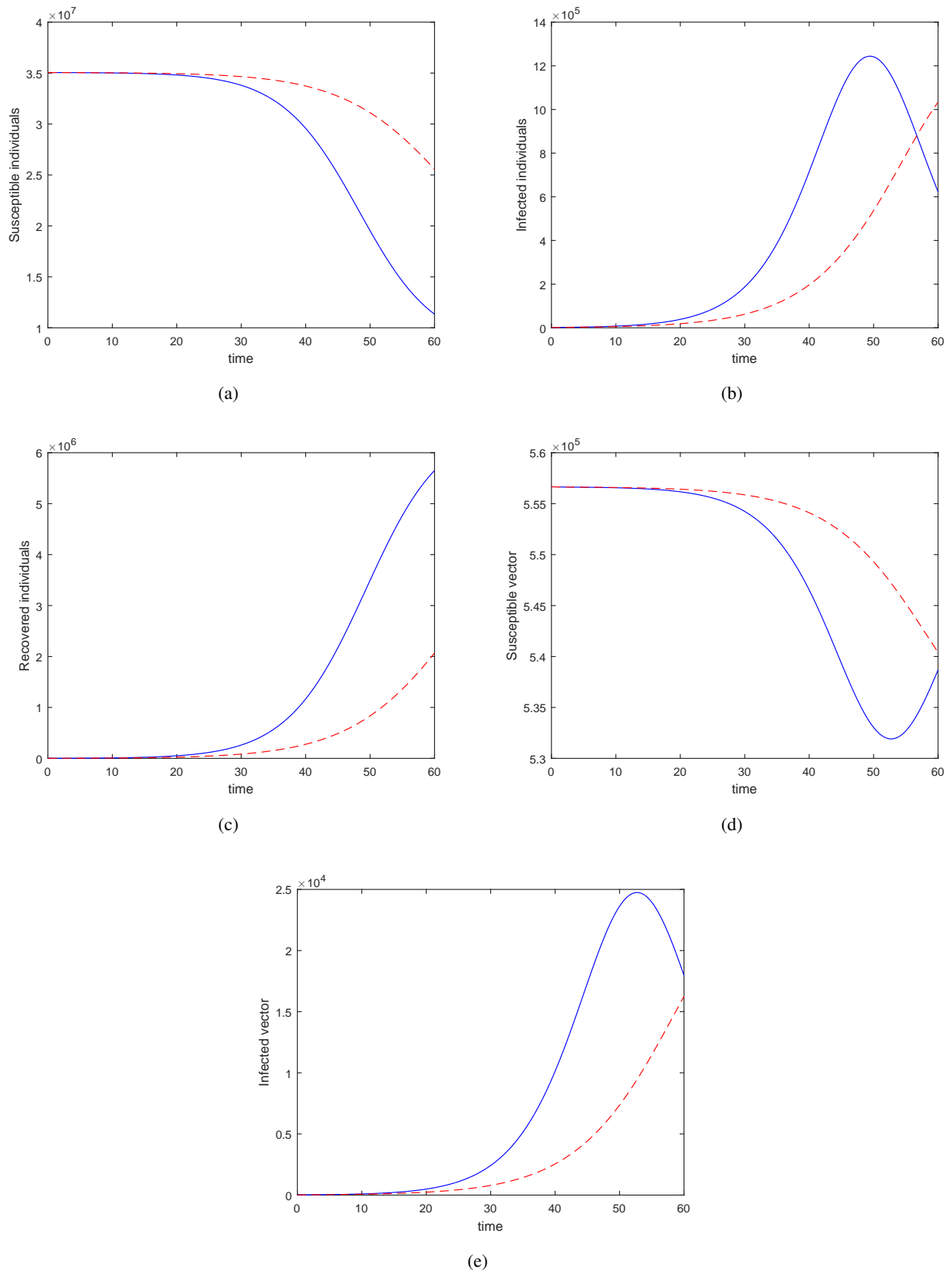


Figure 11. Numerical result for Vector host model (6.2) when $\alpha = 0.9$.

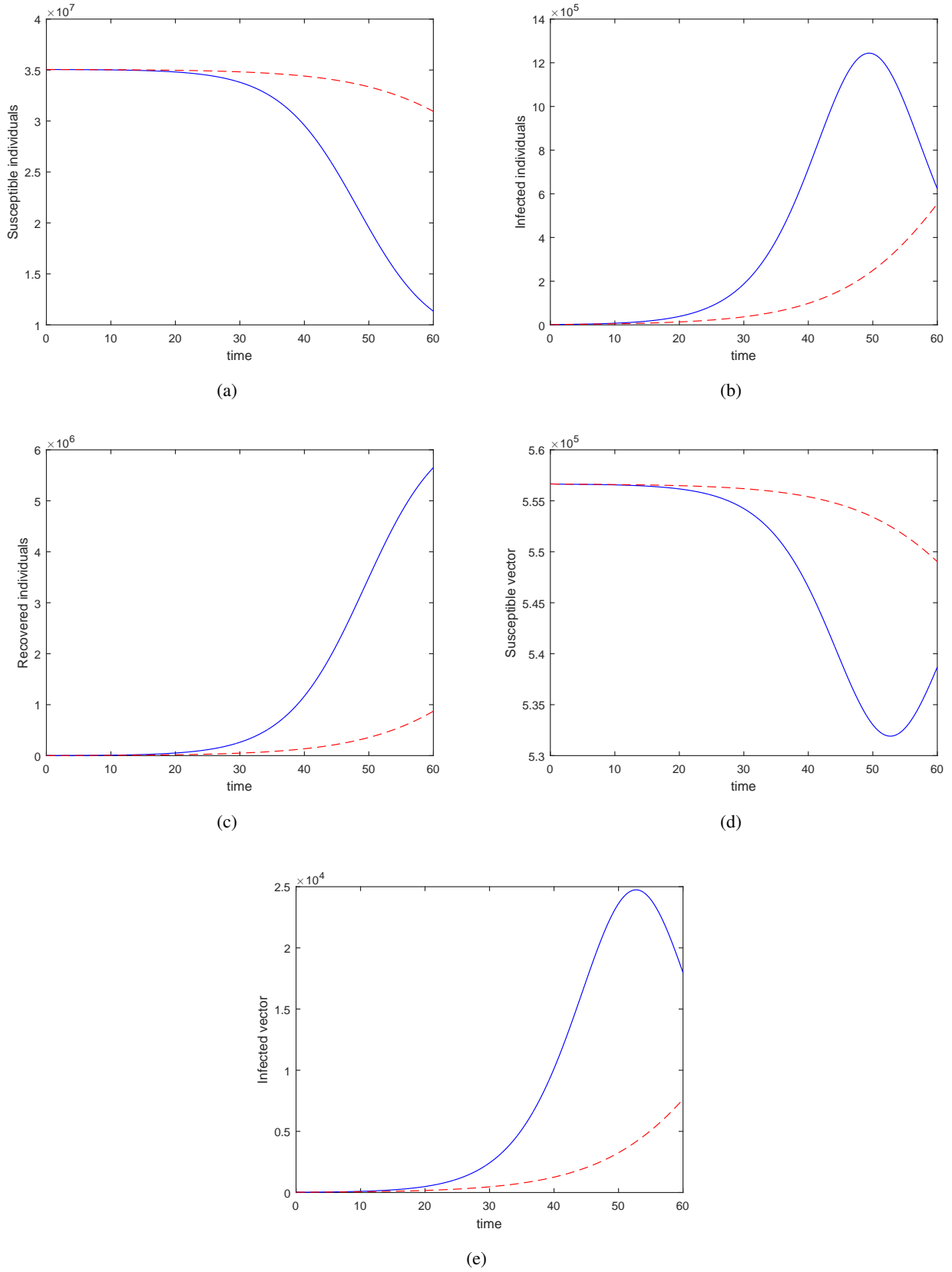


Figure 12. Numerical result for Vector host model (6.2) when $\alpha = 0.85$.

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Conflict of interest

The authors declare that they have no competing interests.

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