

Brian Amanda, 2018, **Analisis Model Matematika Penyebaran Penyakit Cacar Tupai pada Invasi Tupai Abu-Abu ke Tupai Merah**. Skripsi ini di bawah bimbingan Dr. Miswanto, M.Si dan Dr. Windarto, M.Si. Departemen Matematika, Fakultas Sains dan Teknologi, Universitas Airlangga, Surabaya.

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### ABSTRAK

Invasi tupai abu-abu ke tupai merah berdampak pada penyebaran penyakit cacar tupai. Virus cacar tupai tidak memiliki manifestasi klinis yang berarti ketupai abu-abu dikarenakan tupai abu-abu memiliki sistem kekebalan terhadap virus cacar tupai, sebaliknya virus cacar tupai pada tupai merah bersifat sangat mematikan karena tupai merah tidak memiliki sistem kekebalan terhadap virus cacar tupai. Pada skripsi ini, dibahas model matematika penyebaran penyakit cacar tupai pada invasi tupai abu-abu ke tupai merah. Berdasarkan analisis model, diperoleh tujuh titik setimbang yakni titik setimbang kepunahan  $E_0$ , titik setimbang non endemic tupai abu-abu dengan kepunahan tupai merah  $E_1$ , titik setimbang bebas non endemic tupai merah dengan kepunahan tupai abu-abu  $E_2$ , titik setimbang non endemic tupai abu-abu dan tupai merah  $E_3$ , titik setimbang endemik tupai abu-abu dengan kepunahan tupai merah  $E_4$ , titik setimbang endemik tupai merah dengan kepunahan tupai abu-abu  $E_5$ , dan titik setimbang endemik tupai abu-abu dan tupai merah  $E_6$ . Dengan menggunakan metode *Next Generation Matrix* (NGM) diperoleh bilangan reproduksi dasar  $R_0$ . Besaran ini menentukan eksistensi dan kestabilan titik setimbang model. Titik setimbang non endemic  $E_1$ ,  $E_2$ , dan  $E_3$  stabil asimtotis jika  $R_0 < 1$ , titik setimbang kepunahan  $E_0$  serta titik setimbang endemik  $E_4$  dan  $E_5$  stabil asimtotis dengan syarat tertentu, sedangkan titik setimbang  $E_6$  cenderung stabil asimtotis dengan pendekatan bidang fase. Hasil simulasi numeric menunjukkan bahwa laju penyebaran penyakit cacar tupai berpengaruh terhadap pertumbuhan populasi tupai abu-abu dan tupai merah.

**Kata Kunci:** *Model matematika, Tupai, Cacar Tupai, Next Generation Matrix, Kestabilan*

Brian Amanda, 2018, **Mathematics Model Analysis of Squirrel Parapoxvirus Transmission in The Invasion of Grey Squirrel towards Red Squirrel**. This final project was supervised by Dr. Miswanto, M.Si and Dr. Windarto, M.Si. Mathematics Department, Faculty of Science and Technology, Airlangga University, Surabaya.

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### ABSTRACT

The invasion of grey squirrel towards red squirrel affects the transmission of squirrel parapoxvirus. The parapoxvirus does not have meaningful clinical manifestation to the grey squirrel's due to the grey squirrel's have immunity against the squirrel parapoxvirus. In contrast, the virus on red squirrel is deadly due to lack of immunity against the squirrel parapoxvirus. In this thesis, we analyze a mathematical model of squirrel parapoxvirus transmission in the invasion of grey squirrel towards red squirrel. From the model, we obtained seven equilibrium point, those are extinction equilibrium  $E_0$ , non-endemic equilibrium of grey squirrel with red squirrel extinction  $E_1$ , non-endemic equilibrium of red squirrel with grey squirrel extinction  $E_2$ , non-endemic equilibrium of grey squirrel and red squirrel  $E_3$ , endemic equilibrium of grey squirrel with red squirrel extinction  $E_4$ , endemic equilibrium of red squirrel with grey squirrel extinction  $E_5$ , and endemic equilibrium of grey squirrel and red squirrel  $E_6$ . By the Next Generation Matrix (NGM), we obtained basic reproduction ratio  $R_0$ . The magnitude of  $R_0$  will determine the existence and stability of equilibrium points of the model. Non-endemic equilibriums  $E_1$ ,  $E_2$  and  $E_3$  are asymptotically stable if  $R_0 < 1$ , while extinction equilibrium  $E_0$  and endemic equilibriums  $E_4$  and  $E_5$  are asymptotically stable under certain condition. The endemic equilibrium  $E_6$  tends to conditionally asymptotically stable with phase plane method. The numerical simulation shows that the rate of squirrel parapoxvirus transmission affect population growth of grey squirrel and red squirrel.

**Keywords** : *Mathematics Model, Squirrel, Squirrel Parapoxvirus, Next Generation Matrix, Stability*