

Abdul Faliq Anwar, 2019, **Analisis Kestabilan Model Matematika Ko-infeksi Virus Influenza A dan Pneumokokus pada Sel Inang**. Skripsi ini dibawah bimbingan Cicik Alfiniyah, M.Si., Ph.D. dan Dr. Windarto, S.Si., M.Si. Departemen Matematika, Fakultas Sains dan Teknologi, Universitas Airlangga, Surabaya.

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## ABSTRAK

Ko-infeksi virus influenza A dan pneumokokus adalah penyakit yang disebabkan karena sel inang terinfeksi virus influenza A dan bakteri pneumokokus dalam waktu yang sama. Tujuan dari skripsi ini adalah untuk menganalisis kestabilan titik setimbang pada model matematika ko-infeksi virus influenza A dan pneumokokus pada sel inang. Berdasarkan analisis model diperoleh empat titik setimbang, yaitu titik setimbang non endemik ko-infeksi ( $E_0$ ), titik setimbang endemik virus influenza A ( $E_1$ ), titik setimbang endemik pneumokokus ( $E_2$ ) dan titik setimbang endemik ko-infeksi ( $E_3$ ). Dengan menggunakan metode *Next Generation Matrix* (NGM) diperoleh dua nilai bilangan reproduksi dasar, yaitu bilangan reproduksi dasar virus influenza A ( $R_{0v}$ ) dan bilangan reproduksi dasar pneumokokus ( $R_{0b}$ ). Eksistensi dari titik setimbang dan kestabilan lokal titik setimbang bergantung pada bilangan reproduksi dasar. Titik setimbang non endemik ko-infeksi stabil asimtotis lokal jika  $R_{0v} < 1$  dan  $R_{0b} < 1$ , titik setimbang endemik virus influenza A cenderung stabil asimtotis lokal jika  $R_{0v} > 1$  dan  $R_{0b} < 1$ , titik setimbang endemik pneumokokus cenderung stabil asimtotis lokal jika  $R_{0v} < 1$  dan  $R_{0b} > 1$ . Sedangkan titik setimbang endemik ko-infeksi cenderung stabil asimtotis lokal jika  $R_{0v} > 1$  dan  $R_{0b} > 1$ . Dari hasil simulasi numerik menunjukkan bahwa kenaikan jumlah populasi virus influenza A dan pneumokokus mengakibatkan jumlah populasi sel yang terinfeksi virus influenza A dan pneumokokus (ko-infeksi) juga mengalami kenaikan.

**Kata Kunci:** Model Matematika, Virus Influenza A, Pneumokokus, Ko-infeksi, Kestabilan, Sel Inang.

Abdul Faliq Anwar, 2019, **Analysis Stability of Mathematical Model The Co-infection of Influenza A Virus and Pneumococcus in The Host Cell**. This undergraduate thesis is supervised by Cicik Alfiniyah, M.Si., Ph.D. dan Dr. Windarto, S.Si., M.Si. Mathematics Departement, Faculty of Science and Technology, Universitas Airlangga, Surabaya.

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### ABSTRACT

Co-infection of influenza A virus and pneumococcus is caused by influenza A virus and pneumococcus bacteria which infected host cell at the same time. The purpose of this thesis is to analyze stability of equilibrium point on mathematical model within-host co-infection of influenza A and pneumococcus. Based on analytical result of the model there are four equilibrium points, non endemic co-infection equilibrium ( $E_0$ ), endemic influenza A virus equilibrium ( $E_1$ ), endemic pneumococcus equilibrium ( $E_2$ ) and endemic co-infection equilibrium ( $E_3$ ). By Next Generation Matrix (NGM), we obtain two basic reproduction number, which are basic reproduction number for influenza A virus ( $R_{0v}$ ) and basic reproduction number for pneumococcus ( $R_{0b}$ ). Existence of equilibrium point and local stability of equilibrium point dependent on basic reproduction number. Non endemic co-infection equilibrium is locally asymptotically stable if  $R_{0v} < 1$  and  $R_{0b} < 1$ ; influenza A virus endemic equilibrium is locally asymptotically stable if  $R_{0v} > 1$  and  $R_{0b} < 1$ ; pneumococcus endemic equilibrium is locally asymptotically stable if  $R_{0v} < 1$  and  $R_{0b} > 1$ . Meanwhile, the co-infection endemic equilibrium is locally asymptotically stable if  $R_{0v} > 1$  and  $R_{0b} > 1$ . From the numerical simulation result, it was shown that increasing the number of influenza A virus and pneumococcus made the number of population cell infected by influenza A virus and pneumococcus (co-infection) also increased.

**Keyword:** Mathematical Model, Influenza A Virus, Pneumococcus, Co-infection, Stability, Host Cell.